

Uncertainty through the Production Network: Sectoral Origins and Macroeconomic Implications

Matteo Cacciatore¹ Giacomo Candian²

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¹HEC Montreal, Bank of Canada, and NBER

²HEC Montreal and CIRANO

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 - E.g., supply shortages and rising relative prices in key upstream industries
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- NK production network model with time-varying uncertainty to interpret the results

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4. Theory: production linkages central to understanding sectoral effects
 - Lower input demand for suppliers and higher marginal cost for customers (input complementarity)
 - Results hold for both supply- or demand-side driven uncertainty

1. Effects of time-varying uncertainty

Bloom(2009), Berger Dew-Becker Giglio (2020), Cesa-Bianchi Pesaran Rebucci (2020), Christiano Motto Rostagno (2014), Basu Bundick (2017) Bloom Floetotto Jaimovich Saporta-Eksten Terry (2018), Dew-Becker and Giglio (2022), Basu Candian Chahrour Valchev (2023), Alfaro Bloom Lin (2023) ..

- We examine sector-specific uncertainty and study network propagation

2. Macro implications of production networks

Acemoglu Carvalho Ozdaglar Tahbaz-Salehi (2012), Acemoglu Ackigit Kerr (2016), Baqaee Farhi (2019a, b), Carvalho Nirei Saito Tahbaz-Salehi (2020) Barattieri Cacciatore (2023) Barattieri Cacciatore Traum (2023) Kopytov Mishra Nimark Taschereau-Dumouchel (2024) ..

- We focus on the effects of second-moment shocks

3. Sectoral or production network dimensions of uncertainty

Segal (2019), Ma Samaniego (2019), Castelnuovo et al. (2022) Grigoris Segal (2021) Saijo (2025)

- We identify high-frequency sectoral uncertainty shocks that are uncorrelated to first-moment shocks and to uncertainty originating in connected industries

1. Data and Measurement
2. Identification
3. Local Projections and Results
4. Model

Implied Volatility (IV) from OptionMetrics

- Daily firm-level uncertainty: implied volatility of US stock options 1996-2019
- *IV* is the conditional variance of the stock return over the life of the option
- **Attractive features**
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- Different from *realized volatility* (RV): backward-looking, reflecting past price movements (realized first-moment shocks)
- **Focus:** equity-based, at-the-money options with 30-days maturity
 - Firms listed in at least one major U.S. stock exchange
 - Most liquid options; same time horizon as the VIX
 - Options traded for at least 10 years
 - Industries for which option issuers jointly represent > 0.20 of mkt cap
 - 14m observations for 6,345 firms

Measures of Sectoral Uncertainty

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$$IV_{i,d} = \sum_{f \in i} s_{f,i,d-1} IV_{f,i,d}$$

$s_{f,i,d-1}$: previous month market cap share of firm f in industry i on day d
(very similar results with previous year sales share)

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- Monthly measure: last-5-trading days average of $IV_{i,d}$
- Realized vol defined analogously using realized squared returns over month

Panel I: Sectoral Component in Firm Implied Volatility

	No aggregate IV_t control		Aggregate IV_t control	
	Unweighted	Weighted	Unweighted	Weighted
R^2	0.66	0.75	0.25	0.30

Panel II: Contemporaneous Correlations

	Sectoral Unc. (pw)	IP	Aggregate Unc.	Inflation
Sectoral Unc.	0.87	-0.14	0.71	0.02
	(0.74, 0.91)	(-0.30, 0.02)	(0.68, 0.90)	(-0.09, 0.10)

Notes: Panel I: average R^2 from monthly regressions: $IV_{f,i,t} = \alpha_f + \beta_{f,i}IV_{i,t} + \gamma_{f,i}IV_t + \epsilon_{f,i,t}$, where $IV_{f,i,t}$ is the daily firm f 's implied volatility averaged over the last 5 trading days of each month, and $IV_{i,t}$ is the corresponding industry-level measure. Panel II: 10th & 90th in brackets.

- Consider the following local projection at horizon h :

$$\ln X_{it+h} - \ln X_{it-1} = \alpha_{ih} + \beta_h \sigma_{i,t} + \epsilon_{it}$$

$X_{i,t}$: industry's outcome , e.g., employment, prices

$$\sigma_{i,t} = \ln IV_{i,t}$$

- Sectoral uncertainty $\sigma_{i,t}$ is **endogenous**:
 - Sector-specific or aggregate **1st-moment shocks**
e.g., $\uparrow$ commodity prices may $\uparrow$ uncertainty in energy-intensive industries
 - Uncertainty elsewhere**
 - Changes in uncertainty originating in supplier and customer industries
 - Aggregate uncertainty**

Supplier and Customer Industry Uncertainty

- Combine uncertainty measures with 2007 total requirement I-O tables (e.g., Acemoglu et al, 2016)
- **Supplier uncertainty** for industry i :

$$\sigma_{i,t}^S = \sum_k \omega_{ki} \sigma_{k,t},$$

ω_{ki} : fraction of i 's output sourced from the k -th intermediate in Leontief Inverse form.

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- Customer uncertainty for industry i :

$$\sigma_{i,t}^C = \sum_k \tilde{\omega}_{ik} \sigma_{k,t},$$

$\tilde{\omega}_{ik}$: fraction of i 's output demanded by k -th sector in Leontief Inverse form.

Identification Approach – First-Stage Regression

- Purge $\sigma_{i,t}$ of endogenous variation via industry-level time-series regressions:

$$\sigma_{i,t} = \alpha_i + \sum_{\ell=1}^p \varphi_i^{\ell} \sigma_{i,t-\ell} + \sum_{\ell=0}^p \psi_{rv_i}^{\ell} rv_{t-\ell} + \sum_{\ell=0}^p \psi_{\sigma_i}^{\ell} \sigma_{t-\ell} + \sum_{\ell=0}^p \boldsymbol{\psi}_i^{\ell} \mathbf{z}_{i,t-\ell} + v_{i,t}$$

$$\mathbf{z}_{i,t} = [rv_{i,t}, rv_{i,t}^S, rv_{i,t}^C, \sigma_{i,t}^S, \sigma_{i,t}^C]'$$

1. Control for realized volatility (rv): parse out effects of 1st-moment shocks

- rv (1st-moment shocks) can affect uncertainty immediately
- Uncertainty shocks don't affect RV on average as in Berger et al. (2020 ReStud)

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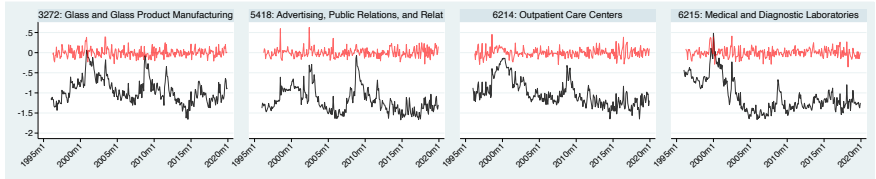
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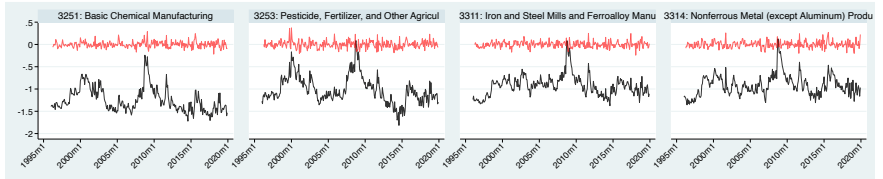
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- Control for aggregate uncertainty

Uncertainty Measures and Shocks

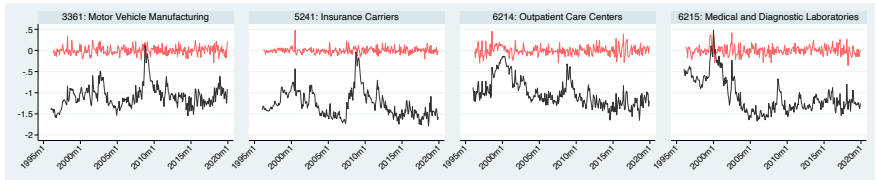
Industries with Largest Shocks' Standard Deviation



Most Upstream Industries



Least Upstream Industries



First-Stage Results: Shocks Properties

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- Estimated shocks have desirable statistical properties
 1. Not autocorrelated
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- Distribution of shock sizes relatively similar upstream and downstream
- What do these shocks capture?
 - Changes in uncertainty common across firms within a NAICS 4-digit industry
 - Idiosyncratic uncertainty affecting large firms within the industry
- Large shocks associated with:
 - Regulatory changes
 - Financial restructuring
 - Technological transformations
 - Trade tensions

- Construct supplier and customer industries shocks as before

$$\hat{v}_{it}^S = \sum_k \omega_{ki} \hat{v}_{kt} \quad \hat{v}_{it}^C = \sum_k \tilde{\omega}_{ik} \hat{v}_{kt}$$

Local Projections

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- Estimate panel local projections: (Jorda, 2005)

$$\ln X_{it+h} - \ln X_{it-1} = \alpha_{ih} + \beta_h^O \hat{v}_{it} + \beta_h^D \hat{v}_{it}^S + \beta_h^U \hat{v}_{it}^C + \omega_{t+h} + \sum_{\kappa=1}^{p_x} \Phi_x^\kappa \mathbf{x}_{t-\kappa} + \epsilon_{it+h}$$

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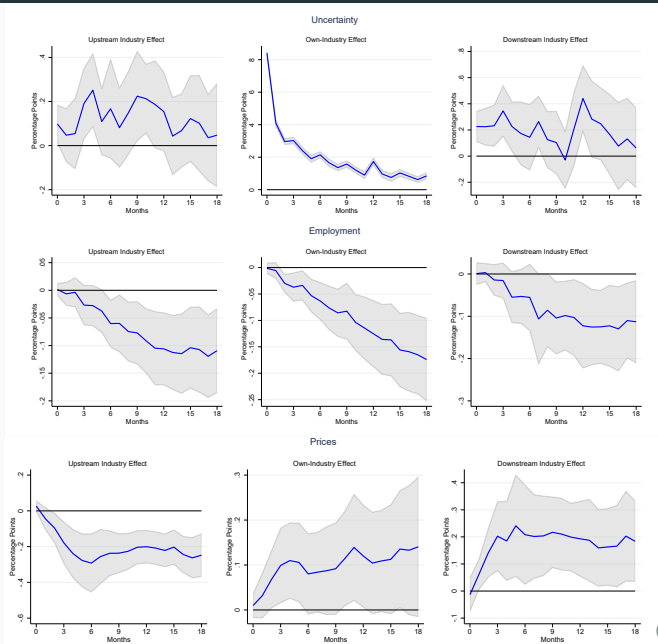
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- Outcome variables (X): **uncertainty, employment, prices**
- $\beta_h^O \equiv$ average own-industry effect at horizon h
- $\beta_h^D \equiv$ average downstream effect at horizon h
- $\beta_h^U \equiv$ average upstream effect at horizon h
- $\mathbf{x}_{t-\kappa} \equiv$ lags of $\ln X_{it} - \ln X_{it-1}$, lags of shocks

Local Projections: Industry-Level Effects



Robustness

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- X: VIX, aggregate employment, Core CPI
- $\mathbf{x}_{t-\kappa}$: lags of $\ln X_t - \ln X_{t-1}$, shocks, RV, shadow rate (Wu and Xia, 2016)

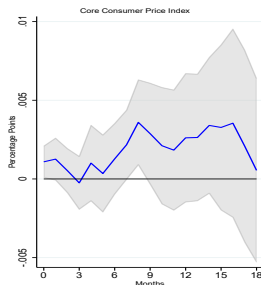
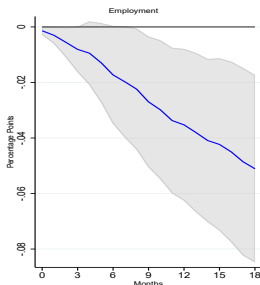
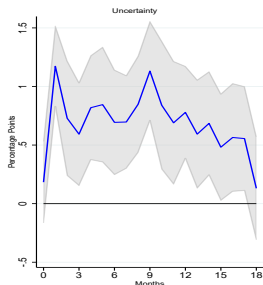
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Aggregate Inflation Effects for Upstream and Downstream Uncertainty

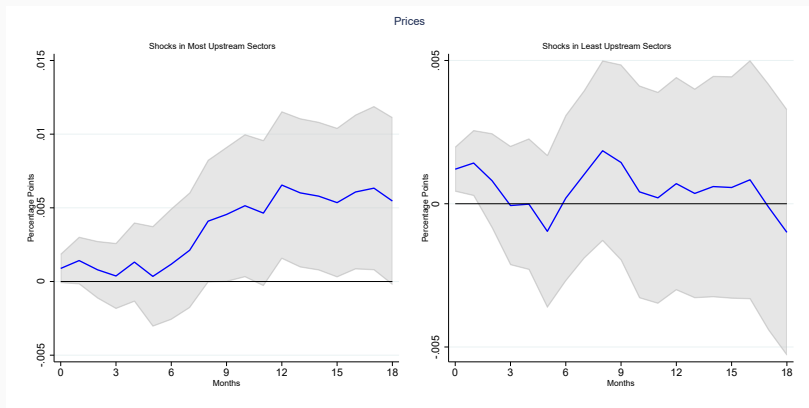
- Does inflation response depend on whether uncertainty originates upstream/downstream?

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NK-IO network model with time-varying volatility

- Households maximize

$$\mathbb{V}_t = \max \left[(1 - \beta)(C_t^{\eta'} (1 - N_t)^{1 - \eta'})^{1 - 1/\psi} + \beta(\mathbb{E}_t \mathbb{V}_{t+1}^{1 - \gamma'})^{\frac{1 - 1/\psi}{1 - \gamma'}} \right]^{\frac{1}{1 - 1/\psi}},$$
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$$Z_{s,t}^j = \left[\alpha_s^{\frac{1}{\vartheta_s}} (\textcolor{red}{A}_{s,t} N_{s,t}^j)^{\frac{\vartheta_s-1}{\vartheta_s}} + (1 - \alpha_s)^{\frac{1}{\vartheta_s}} (\textcolor{teal}{H}_{s,t}^j)^{\frac{\vartheta_s-1}{\vartheta_s}} \right]^{\frac{\vartheta_s}{\vartheta_s-1}} \quad \text{with} \quad \textcolor{teal}{H}_{s,t} = \prod_{x=1}^S H_{s,x,t}^{\omega_{h,s,x}}.$$

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- Monetary policy: $\log(R_t/R) = \rho_i \log(R_{t-1}/R) + (1 - \rho_i)\psi_\pi \log(\Pi_t/\Pi)$
- Exogenous processes:

$$\log A_{s,t} = (1 - \rho_a) \log A_s + \rho_a \log A_{s,t-1} + \sigma_{s,t-1}^a \varepsilon_{s,t}^a$$

$$\sigma_{s,t}^a = (1 - \rho_{\sigma_a}) \log \sigma^a + \rho_{\sigma_a} \log \sigma_{s,t-1}^s + \sigma_{\sigma_a} \varepsilon_{s,t}^\sigma$$

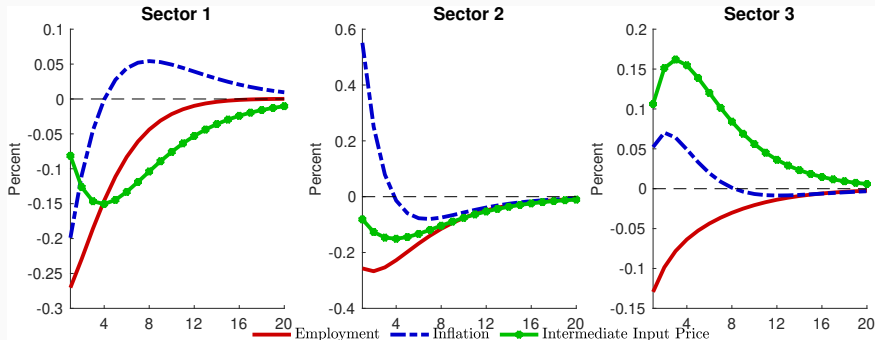
Impulse Responses to Sectoral Uncertainty Shock

- Study propagation of sectoral uncertainty shocks in a 3-sector case
 - Linear network for intuition ($S1 \rightarrow S2 \rightarrow S3$);
 - Uncertainty shock in $S2$

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(a) Baseline Network



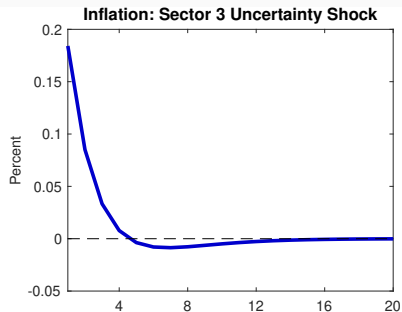
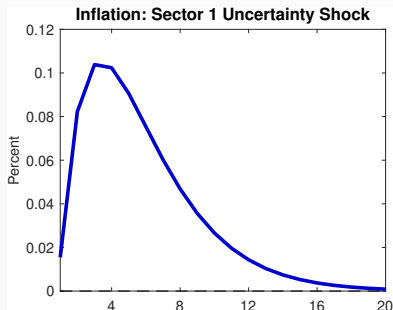
Supply vs Demand Uncertainty

Complementarity

Aggregate Shock

Aggregate Inflation Response

- Aggregate inflation response depends on sectoral origin of uncertainty



- Regardless of the source of uncertainty (supply- vs demand-side):
 - Higher prices and lower input demand where uncertainty increases
 - Lower input demand in the upstream sector (deflationary)
 - Price pass-through downstream (inflationary)
- These effects dominate other GE forces
(e.g., wealth effects on labor supply, precautionary savings)
- Aggregate inflation response depends on sectoral origin of uncertainty

- Uncertainty shocks are significantly transmitted along the supply chain
 - Transmit upstream like a negative demand shock
 - Propagate downstream like an adverse supply shock
- Aggregate effects are contractionary; inflationary if uncertainty originates upstream
- NK production network model rationalizes the empirical estimates

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- NK production network model rationalizes the empirical estimates
- Implications for macro policy design
 - Uncertainty arising upstream intensifies the inflation-output tradeoff
 - Uncertainty may exacerbate or dampen the inflationary impact of first-moment shocks (e.g., supply disruptions, demand shortfalls)

Thank you!

giacomo.candian@hec.ca

Measuring Sectoral Uncertainty

- Start from sector- i version of CAPM:

$$r_{f,t+1} = \beta_{f,i} r_{i,t+1} + \epsilon_{f,t+1} \quad \text{where} \quad r_{i,t+1} \equiv s_{f,i,t} r_{f,t+1}$$

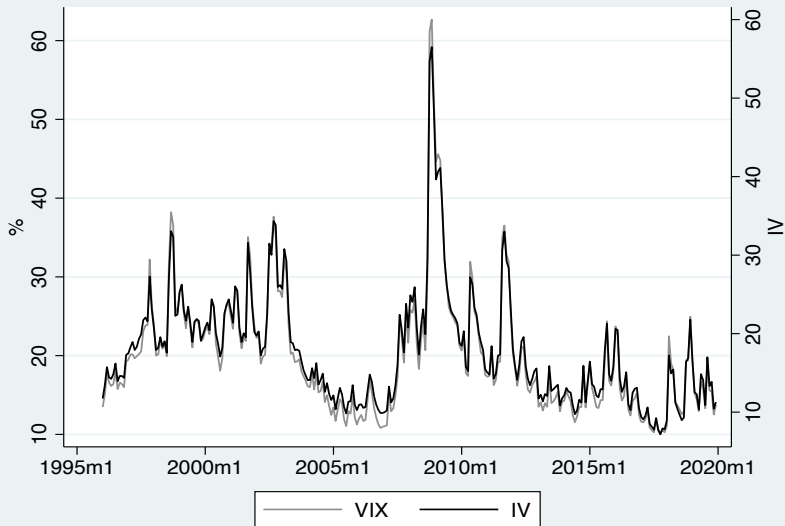
- Take conditional variance:

$$\sigma_{f,t}^2 = \beta_{f,i}^2 \sigma_{i,t}^2 + \sigma_{\epsilon,i,t+1}^2$$

- Following Campbell et al. (2001), using $\sum_f s_{f,i,t} \beta_{f,i} = 1$, one can show:

$$\sum_f s_{f,i,t} \sigma_{f,t}^2 = \underbrace{\sigma_{i,t}^2}_{\text{common uncertainty}} + \underbrace{\sum_f s_{f,i,t} \sigma_{\epsilon,i,t+1}^2}_{\text{average id uncertainty}}$$

Aggregate Implied Volatility vs VIX

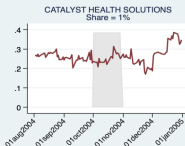
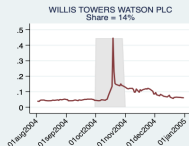
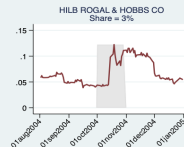
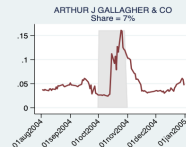
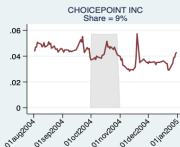
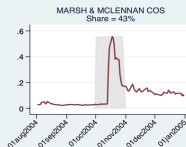


Examples

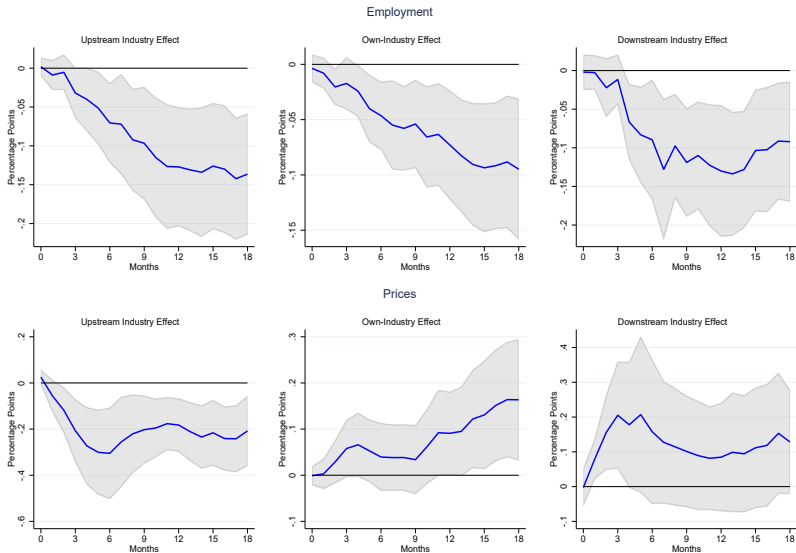
- **Insurance industry** (5241), October 2004. Antifraud investigation by the NY attorney general led many insurance companies to announce they would stop paying contingent commissions to their agents.
- **Outpatient care industry** (6214), series of large shocks in 2015. At this time, the Centers for Medicare & Medicaid Services began implementing value-based care initiatives. Outpatient care centers faced uncertainties in adapting to these new business models.
- **Motor vehicle manufacturing industry** (3361), important spike in 1998 when Daimler-Benz AG acquired Chrysler Corporation. This merger represented a major consolidation in the automotive industry.
- **Ferrous and non-ferrous metal industries** (3311 and 3314) rising uncertainty during the late 2010 ' following US-China escalating trade tensions.
- **Advertising industry** (5418). Shock series captures key events that transformed the sector: digital shift of the late 1990s, launch of Google AdWords in Oct 2000, and launch of YouTube in Feb 2005.

Shocks: Agencies, Brokerages, and Other Insurance Related Activities

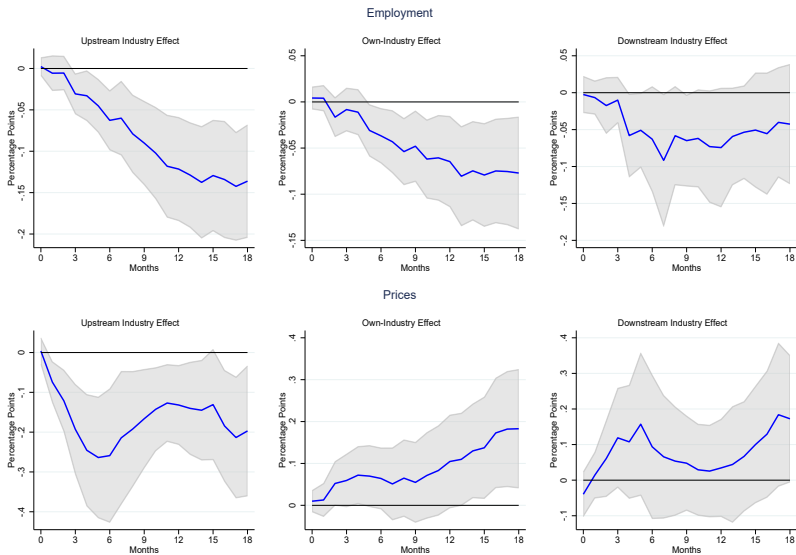
Industry 5242



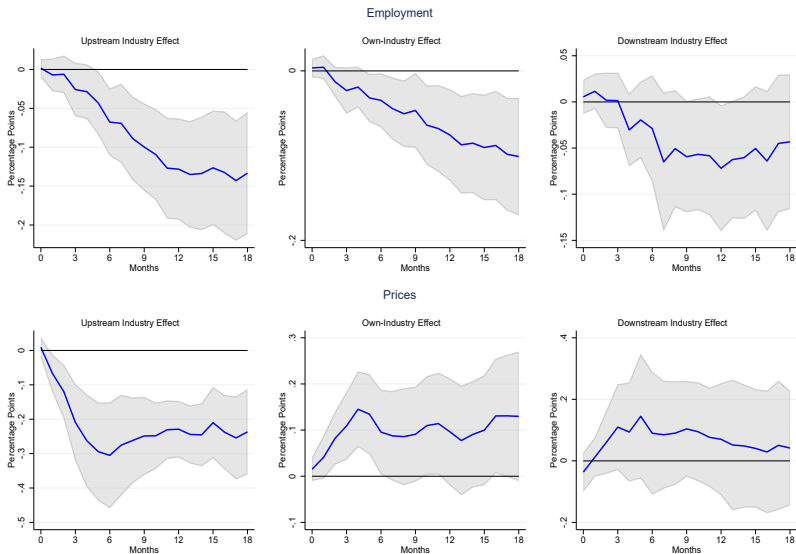
Robustness - Responses to an Uncertainty Shock - Sales Weights



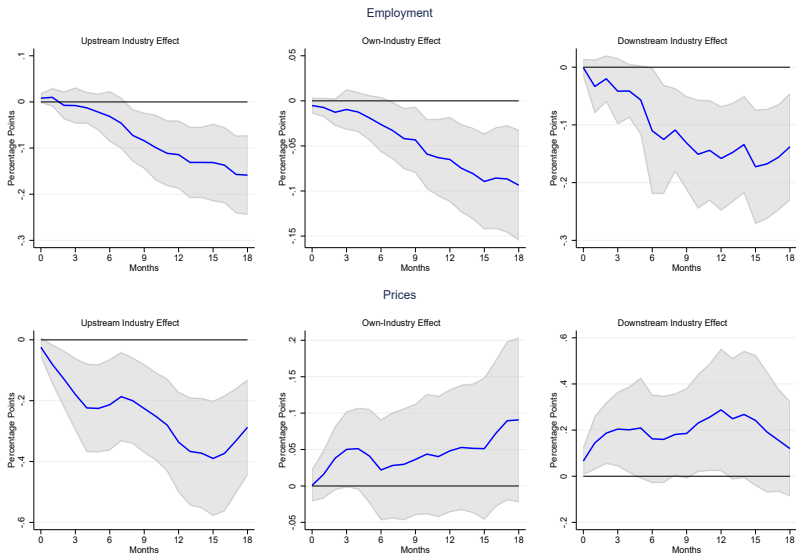
Robustness - Responses to an Uncertainty Shock - Fixed Effect



Robustness - Responses to an Uncertainty Shock - Options Traded > 5 Years

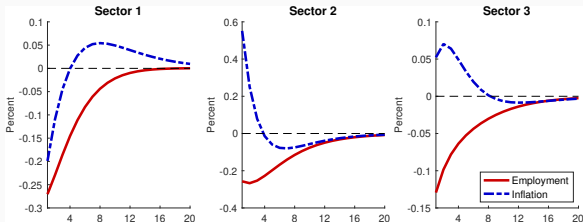


Robustness - Responses to an Uncertainty Shock - Simple First Stage

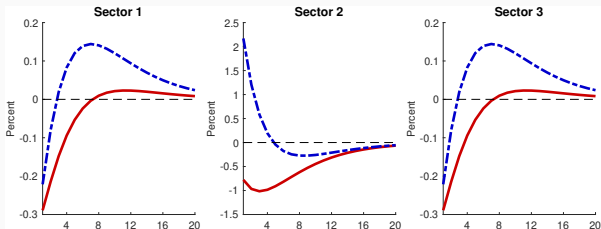


Baseline vs No Network Economy

(a) Baseline Network

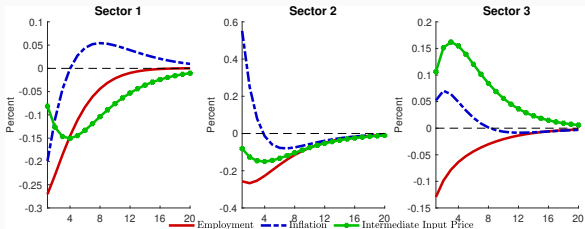


(b) No Network

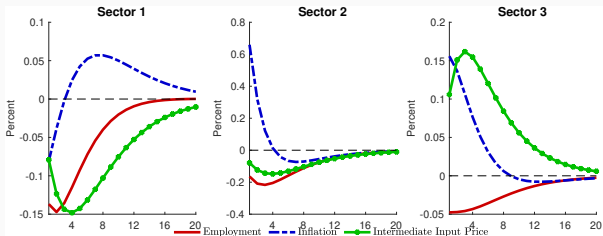


Baseline vs No Precautionary Savings

(a) Baseline Network

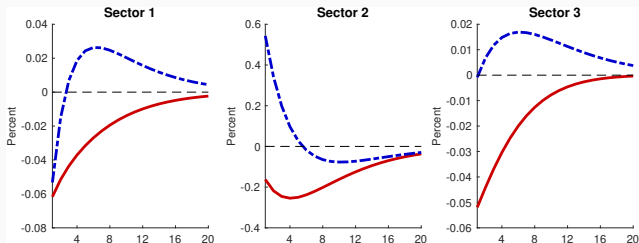


(b) No Precautionary Savings

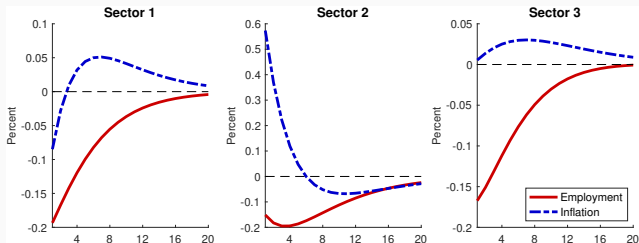


Robustness: Supply vs Demand Uncertainty Shocks

(a) Empirical Network - Supply Uncertainty Shock

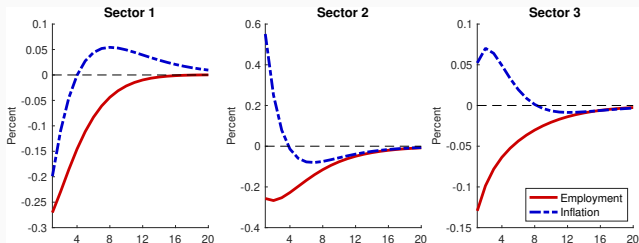


(b) Empirical Network - Demand Uncertainty Shock

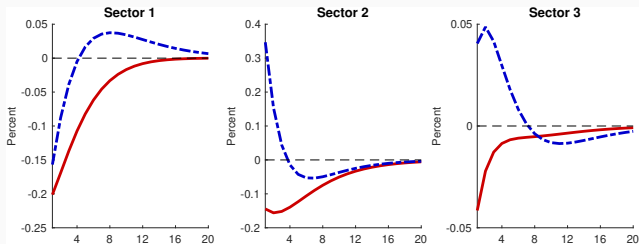


Robustness: Complementarity in Production Function

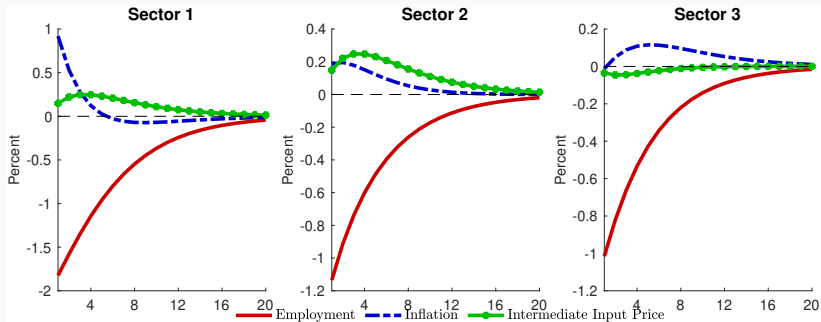
(a) Baseline ($\vartheta = 0.5$)



(b) Cobb Douglas Production ($\vartheta = 1$)



Aggregate Uncertainty Shock



Back