

# Real versus Financial Frictions to Capital Investment<sup>α</sup>

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## Abstract

We examine the investment behavior of a panel of German manufacturing firms for the time period from 1992 to 2000. Our methodology is structural and has several steps: First, we identify the profitability shocks that move investment demand at the firm level. Then, we specify an array of adjustment costs and capital market imperfections possibly influencing optimal firm investment response to these shocks. Finally, we use an indirect inference procedure as in Gourieroux, Monfort and Renault (1993) and Smith (1993) to estimate the structural parameters. Our goal is to characterize the relative importance of financing constraints and various costs of adjustment in German manufacturing.

Keywords: investment, indirect inference, panel data .

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# 1 Introduction

Investment is an important component of aggregate activity and much effort has been spent on trying to understand it. The workhorse of modern investment research has been Tobin's Q theory and the neoclassical theory of investment with convex adjustment costs.<sup>1</sup> In this framework, the market value of capital is an important determinant of a firm's capital investment decision. It is fair to say that the initial empirical results of this research have been largely disappointing. Briefly, the estimates of investment responsiveness to fundamentals have been very low whereas output terms (such as profits) have been very significant contrary to theoretical implications. This has continuously set a challenge on empirical work.

The research of the last fifteen years has experienced two breakthroughs. In reverse chronological order, one emphasizes the importance of nonlinearities and the other of financing constraints. Below we review briefly these two influential strands.

## Nonlinearity

This literature argues that the apparent failures of neoclassical theory are a result of misspecification of the costs that are relevant in the capital adjustment decision. In particular, irreversibilities and fixed costs to investment may lead firms to experience episodes of zero investment as well as episodes of large investment in response to similarly small movements in fundamentals. This is in sharp contrast to convex adjustment costs which, at least in their usual quadratic implementation, imply proportional responses. This provides an explanation for the low estimated responsiveness in the data of investment to fundamentals.<sup>2</sup>

One of the first empirical contributions in this mold is Doms and Dunne (1998) who show that in a sample of U.S. manufacturing establishments about 25 percent of a typical establishment's total investment over 17 years is concentrated in a single year. Caballero, Engel and Haltiwanger (1995) and Caballero and Engel (1999) show that investment response to fundamentals, measured by the gap between actual and desired capital stock, is

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<sup>1</sup>See Tobin (1969), Lucas and Prescott (1971), Mussa (1977), Hayashi(1982), Abel (1983) for seminal contributions as well as Abel (1990) for a review and link to Jorgenson's (1963) user cost concept.

<sup>2</sup>The role of irreversibilities was stressed by Dixit and Pindyck (1994), Bertola and Caballero (1994), and Abel and Eberly (1996), among others. The role of fixed costs was stressed by Abel and Eberly (1994), Caballero and Leahy (1996), and Caballero and Engel (1999), among others.

disproportionately larger for a larger gap. Cooper, Haltiwanger and Power (1999), Schiantarelli and Nilsen (1999) provide evidence that the hazard of a large investment “spike” is increasing in the years since the last investment “spike.” Barnett and Sakellaris (1998), Barnett and Sakellaris (1999), and Abel and Eberly (2002a) ...nd that investment responsiveness to Tobin’s Q is highly non-linear. Finally, Ramey and Shapiro (2001) ...nd that for some plants in the US aerospace industry the discounts on reselling capital assets average 25 percent. All this evidence is consistent with important non-convex adjustment costs. An influential paper by Cooper and Haltiwanger (2002) provides structural estimates supporting the existence of both convex and ...xed costs in plant-level investment activities in US manufacturing.

In summary, some lessons from this literature are that: 1) Tobin’s Q is quite informative for investment once nonlinearity is allowed, and 2) it is not warranted to give structural adjustment cost interpretation to coefficients based on regressions of investment on Q.<sup>3</sup>

#### Financing constraints

Firms rely mainly on internal sources of funds to ...nance investment.<sup>4</sup> This has been interpreted as evidence of a divergence between the costs of internal and external funds. Early theories leading to such a cost wedge or, even, rationing of external funds invoked the existence of information asymmetries or agency problems. The importance of internal funds in predicting aggregate investment has been recognized at least since Meyer and Kuh (1957). However, Fazzari, Hubbard and Petersen (1988) has been instrumental in connecting this observation to ...nancial market imperfections and testing it at the ...rm level. Their basic working hypothesis is that the sensitivity of investment to cash flow should be higher for ...rms that face a larger wedge in the cost of internal and external funds(monotonicity hypothesis). They argue they could identify a priori liquidity constrained ...rms and then demonstrated for these a high sensitivity of investment to cash flows. On the other hand, Tobin’s Q appears to have only a marginal impact on investment for these ...rms.<sup>5 6</sup>

<sup>3</sup>Abel and Eberly (2002b, and c) provide some fresh models resulting in the second lesson above.

<sup>4</sup>Ross, Wester...eld and Jordan (1999) document that ...rms raise more than 80 percent of equity from internal sources.

<sup>5</sup>A voluminous literature followed them in this approach including Hoshi, Kashyap, and Scharfstein (1991) for Japanese ...rms. See Schiantarelli (1996) and Hubbard (1998) for a survey.

<sup>6</sup>A parallel literature has examined inventory investment behavior arguing for the importance of ...nancing constraints in explaining the dramatic cycles in inventory investment. See Kashyap, Lamont and Stein (1994)

Kaplan and Zingales (1997), however, have questioned the validity of this approach for testing the existence of financing constraints. They argue that the monotonicity hypothesis is not a necessary prediction of a model of optimal investment under financial constraints. They also question several of the methods used in the literature to identify a priori liquidity constrained firms.<sup>7</sup>

Other criticisms have arisen too. Gomes (2001) demonstrates that the existence of financing constraints is not sufficient to establish cash flow as a significant regressor in standard investment regressions that include Q. Furthermore, financing constraints are not necessary to obtain significant cash flow coefficients either. Empirical work by Erickson and Whited (2000) demonstrates that the sensitivity of investment to cash flow in regressions including Tobin's Q is to a large extent due to measurement error in Q. Cooper and Ejarque (2002) demonstrates that the statistical significance of cash flow in a standard Q investment regression may reflect firm market power rather than financing constraints.<sup>8</sup> Abel and Eberly (2002b) have a similar theoretical point in the absence of any adjustment cost.

We should make clear that none of these criticisms actually disprove the importance of financing constraints in influencing firm investment. Their message is that the use of reduced-form investment regressions where Tobin's Q is meant to control for fundamentals and cash flow to pick up the influence of financial market imperfections is dubious.

Some other work has followed different methods in testing for the presence of financing constraints. A sizable strand of the literature, starting with Whited (1992), Bond and Meghir (1994), and Hubbard and Kashyap (1992) has used the investment Euler equation to test whether internal funds affects the firm's incremental intertemporal investment allocation.<sup>9</sup> Gilchrist and Himmelberg (1999) construct a measure of marginal Q as well as a measure of financial factors and include them in investment regressions. Hu and Schiantarelli (1998) estimate an explicit switching regressions models for investment. Whited (2002) ex-

and Carpenter, Fazzari and Petersen (1998) among others.

<sup>7</sup>See also Fazzari, Hubbard and Petersen (2000) and Kaplan and Zingales (2000) as part of the debate that ensued in the literature.

<sup>8</sup>In a related paper, Galeotti and Schiantarelli (1991) have demonstrated that monopolistic competition introduces output in the investment equation in addition to Q.

<sup>9</sup>There are numerous other papers using this approach. Among these are Hubbard, Kashyap and Whited (1995), and Jaramillo, Schiantarelli and Weiss (1996).

amines investment hazard: the probability of undertaking a large investment project as a function of the time since the last project. These papers find support for the hypothesis that financial constraints affect firm investment.

What should be clear from the above discussion is that we are desperately in need of structure in investigating investment. This structure should allow for the existence of both convex and non-convex adjustment costs and specify the channel through which financial frictions bite. In this paper, we formulate such a theoretical model, estimate, and evaluate it. In so doing we are moving beyond simply testing and rejecting a neoclassical model without frictions and instead attempt to provide quantitative estimates of the importance of different frictions, real and financial, on firm investment. In our structural model financial imperfections enter through a premium on the cost of debt that depends on the firm's leverage ratio. Bernanke, Gertler and Gilchrist (1999) review the literature that provides theoretical justification for this formulation.

We estimate the model using indirect inference as proposed by Gourieroux, Monfort and Renault (1993) and Smith (1993). This method involves picking some appropriate regression coefficients or data moments as "benchmarks" that we would like the model to match well. Then, the structural parameters are estimated so that the model, when simulated, generates "benchmarks" as close to those of the actual data as possible. The method is very flexible in allowing the use of a wide selection of "benchmarks." Care needs to be taken, however, so that appropriate ones are selected. Our benchmark is an investment regression involving linear and non-linear terms in shocks to profitability and debt leverage.

We intend to address in this paper questions for German Manufacturing investment such as the following: 1) What is the relative magnitude of excess cost to debt finance? 2) Is the responsiveness of aggregate investment to aggregate profitability conditions moderated by financing constraints? If so, by how much? 3) What percent of operating profits is expended on the costs of adjusting capital? This is just a partial list of interesting questions that we hope to address. We also intend to construct similar data sets of firm level observations for other euro area countries so that we can make a comparative study of the environment for business investment.

## 2 Model

We model a monopolistically competitive firm. In the beginning of period  $t$ ; firm  $i$  has real capital stock,  $K_{it}$ , which reflects all investment decisions up to last period, and net financial liabilities,  $B_{it}$ , which includes both financial assets and liabilities (debt, cash, retained income etc.). If  $B_{it}$  is positive, it reflects the debt stock borrowed last period. On the other hand, if  $B_{it}$  is negative, it is retained income that was invested in assets bearing a risk-free return of  $r$ , the risk-free market interest rate. We assume that debt contracts are written for one period and, similarly, financial assets have a one-period term. Before making any investment decision, the firm observes the current period aggregate and idiosyncratic profitability shocks. Given these state variables, the firm decides on investment and on the amount of debt that needs to be borrowed (or on the amount of dividend retention). The behavioral assumption we maintain is that firm managers maximize the present discounted value of dividends,  $D_{it}$ ; paid out to shareholders.

Profits

The firm's operating profits are given by the following expression:

$$\pi(A_{it}; K_{it}) = A_{it} K_{it}^{\mu} \quad (1)$$

where  $0 < \mu < 1$ ; reflecting the degree of monopoly power.<sup>10</sup>  $A_{it}$  is the current period profitability shock. It contains both an idiosyncratic component,  $\epsilon_{it}$ , as well as an aggregate one,  $A_t$ .<sup>11</sup> The buying price of capital,  $p$ ; is assumed to be constant. We also assume that capital is the only quasi-fixed factor of production, and all variable factors, such as labor and materials, have already been maximized out of the problem. The discount factor,  $\beta$ ; is fixed. The implied discount rate is assumed to be greater than  $r$ , the market interest rate at which the firm can lend.

<sup>10</sup>This functional form of the operating profit function is valid under the assumptions of constant-returns-to-scale Cobb-Douglas production function, constant-elasticity demand function, and flexible labor and materials inputs. Alternatively, it could be derived from a decreasing-returns-to-scale Cobb-Douglas production function under perfect or imperfect competition, though this is not the approach we take in our implementation.

<sup>11</sup>The profitability shock is a function of technology, demand, wage and materials cost shocks as well as structural parameters. Following Cooper and Haltiwanger (2002), we assume that  $A_t$  is a first-order, two state Markov process with  $A_t \in \{A_H, A_L\}$  where  $h$  and  $l$  denotes high and low value of shocks. The idiosyncratic shock is also a first-order Markov process and in our empirical work it takes eleven possible values.

## 2.1 Adjustment Costs

The firm faces various costs when adjusting its capital stock. Our model is general enough to accommodate both convex and non-convex adjustment costs.

### Convex costs

We employ the assumption of a quadratic function, which is common in the literature when describing convex adjustment costs:  $\frac{\phi}{2} \left( \frac{I_{it}}{K_{it}} \right)^2 K_{it}$ . The parameter  $\phi$  affects the magnitude of total and marginal adjustment costs. The higher is  $\phi$  the higher is the marginal cost of investing and the lower is the responsiveness of investment to variations in the underlying profitability of capital.

### Fixed costs

We also allow for the possibility that there is a component of costs that is fixed when investment is undertaken regardless of the investment's magnitude:  $F K_{it}$ . In order for this cost to be relevant at all stages of a firm's life we assume that it is proportional to a firm's size as measured by its capital stock. The parameter  $F$  determines the magnitude of fixed costs.

### Partial Reversibility

Finally, we allow for the presence of a wedge between the selling and buying prices of capital, namely  $p_S \cdot p$ :

## 2.2 Financial Market Imperfections

Firms may finance investment out of their retained earnings or by raising funds in the capital markets. Retained funds consist of current operating profits,  $\pi (A_{it}; K_{it})$ ; or net financial assets carried over from last period. We assume here that the only source of external finance is through debt and that no new equity may be issued by the firm. In the presence of financial market imperfections, there might be a cost advantage to using internal funds as opposed to external ones. In particular, the cost of borrowing may be higher than the risk-free market interest rate. This external finance premium will depend on the firm's financial health, which may be captured by the ratio of its net worth to total assets. Assuming that capital is the only collateral asset that the firm has then financial health may be measured by the leverage ratio,  $\frac{B_{it}}{p_S K_{it}}$ ; that is the ratio of debt to the resale value of capital. We assign

the following functional form to the external finance premium:<sup>12,13</sup>

$$\hat{r}_{it}(K_{it}; B_{it}) = \theta \frac{B_{it}}{p_S K_{it}} \quad (2)$$

Note that this premium exists only when  $B > 0$ : The firm's lending rate is unaffected. The coefficient  $\theta$  determines the magnitude of external finance premium, and, in turn, the magnitude of the financial market imperfections. The expected sign of  $\theta$  is non-negative. This means that firms maintaining a higher leverage ratio need to pay higher premia. The restriction that no new equity may be issued by the firm or, alternatively, that debt be the marginal source of external finance is introduced through a non-negativity constraint on dividends. We don't think that restricting the firms external finance to only debt and excluding equity is too severe. For most German firms the marginal external source of funds is debt. An ECB study (ECB, 2002) suggests that loans are by far the most important source of external finance. During the period 1998-2000, external financing through new loans averaged 6.7% of GDP. In contrast the gross amount of capital raised by new shares (both listed and non-listed) amounted to 1.3 percent in 1998 (and 1.2 of GDP in 2000).

## 2.3 Value maximization

The firm manager's dynamic program can be written as follows:

$$V^a(A_{it}; K_{it}; B_{it}) = \max \{ V^b(A_{it}; K_{it}; B_{it}); V^s(A_{it}; K_{it}; B_{it}); V^{na}(A_{it}; K_{it}; B_{it}) \} \quad (3)$$

In words, the manager needs to choose optimally between buying capital, with value  $V^b$ ; selling capital, with value  $V^s$ ; or undertaking no investment at all, with value  $V^{na}$ . The value of each one of these discrete choices, ( $j = b; s; na$ ); is in turn defined as follows:

<sup>12</sup>There might be some concerns about whether high debt indicates that a firm faces with financial problems or it shows that firms have perfect access to the debt market so that they have such a high level of debt. Many studies assume that high debt stock relative to the capital stock is an indicator that firms are financially vulnerable since their net worth is low. Some examples of these studies are: Bernanke and Gertler (1990), Bernanke, Campbell and Whited (1990), Whited (1992), Hu and Schiantarelli (1998), and Gilchrist and Himmelberg (1998). When firms are financially fragile, lenders will take higher risk by lending funds to these firms, so they will charge a higher external finance premium to compensate this risk.

<sup>13</sup>Gilchrist and Himmelberg (1998) use this kind of external finance premium. But they do not assign any functional form to it. Jaramillo, Schiantarelli, and Weiss (1996) use an explicit form of external finance premium, which is linear in the leverage ratio.

$$V^j(A_{it}; K_{it}; B_{it}) = \max_{fK_{it+1}; B_{it+1}} D_{it} + \beta E_{A_{it+1}|A_{it}} V^j(A_{it+1}; K_{it+1}; B_{it+1}); \quad (4)$$

subject to (1), (2) and the following constraints:

$$D_{it} = \begin{cases} \beta [A_{it}; K_{it}] - C^j(K_{it}; I_{it}) + B_{it+1} - (1+r)(1+\gamma_{it}(K_{it}; B_{it}))B_{it} & \text{when } B_{it} > 0 \\ \beta [A_{it}; K_{it}] - C^j(K_{it}; I_{it}) + B_{it+1} - (1+r)B_{it} & \text{when } B_{it} < 0 \end{cases} \quad (5)$$

$$I_{it} = K_{it+1} - (1-\delta)K_{it} \quad (6)$$

$$D_{it} \geq 0 \quad (7)$$

where  $V^j(\cdot)$  is the value function,  $\beta E_{A_{it+1}|A_{it}} V^j(\cdot)$  is the present discounted future value of the firm,  $\gamma_{it}(\cdot)$  is the external finance premium,  $C(\cdot)$  is the investment cost function,  $I_{it}$  stands for investment,  $\delta$  is the depreciation rate, and  $i, t$  are firm and time indexes respectively.

The investment cost, captured by the function  $C(\cdot)$ ; depends on the manager's discrete choice. In the case of positive investment,  $j = b$ ; it contains the purchase cost as well as fixed and convex adjustment costs:

$$C^b(K_{it}; I_{it}) = pI_{it} + \frac{\phi}{2} \frac{I_{it}^2}{K_{it}} K_{it} + F K_{it} \quad (8)$$

When the firm sells capital,  $j = s$ ; the costs are:

$$C^s(K_{it}; I_{it}) = p_s I_{it} + \frac{\phi}{2} \frac{I_{it}^2}{K_{it}} K_{it} + F K_{it} \quad (9)$$

Finally, when no action is undertaken regarding investment,  $j = na$ ; the investment costs are zero:

$$C^{na}(K_{it}; I_{it}) = 0 \quad (10)$$

In summary the set of structural parameters is:  $\beta; \delta; \mu; \phi; F; p_b; p_s; \gamma$ : These together with the transition matrix for the profitability shocks ( $A_{t+1}$ ) determine the behavior of the model.

## 3 Empirical results

### 3.1 Data set

Our data are an unbalanced panel of 170 German manufacturing firms over the period 1992-1999 containing 1163 observations. The data is derived from the AMADEUS database. The firms are not an unbiased sample of the total manufacturing population, rather they are drawn from the largest German manufacturing firms.<sup>14</sup> This is mainly because data was not available for smaller manufacturing firms.<sup>15</sup> The median firm had a capital stock of 133 million euros (in 1995 prices). Although the sample contains only 170 firms, they represent more than 20% of the manufacturing industry capital stock. They had a total replacement value of capital stock of 101 billion euro in 1995, where the total manufacturing industry in Germany had in 1995 a capital stock total of 483 billion euro. The median investment rate is relatively high at 0.16. Although we succeeded in deleting firm observations from the data when the investment figure entailed substantial merger or acquisition activity (rather than the buying of new equipment or buildings), we were not able to identify every possible acquisition. So the investment rate probably includes some acquisitions or mergers.

Table 1 shows further summary statistics of the data. Table 2 shows some features of the investment rate. Around 0.7% of the observations entail an investment rate near zero (defined as less than 1% in absolute value). At first sight this looks small, compared to e.g. Cooper and Haltiwanger (2002) who state that for US manufacturing plants the inaction rate is 8%. However given that our firms are practically certainly operating multiple plants, a lower inaction rate is not surprising. (For instance suppose each firm has only two plants with each an inaction rate of 8%, and assume the inaction periods are uncorrelated. This would lead to a firm inaction rate of approximately 0.6%.) Around 4.7% of the investment rates are negative (as a comparison it is 10.4% in Cooper and Haltiwanger 2002). 38% of the investment observations are above 20%.

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<sup>14</sup>Our final sample contains the very large well know firms as e.g. bayer, basf, Volkswagen, bmw and adidas-salomon, but contains also much smaller (but still relatively large) less well know firms as schwabenverlag, Aqua signal, Buckau Walter.

<sup>15</sup>For more details on sample selection see the appendix

Table 1. Summary Statistics

	mean	median	st.dev	min	max
$I_{it}=K_{itj-1}$	0.19	0.16	0.16	-0.50	0.88
$K_{it}$	661	133	2194	2	26000
$CF_{it}=K_{itj-1}$	0.30	0.23	0.41	-0.84	3.44

capital stock is in million euros measured in 1995 prices.

Table 2. Features of the distribution of the investment rate

$j I_{it}=K_{itj-1}  < 0:01$	0.9%
$j I_{it}=K_{itj-1}  < 0:02$	3.3%
$I_{it}=K_{itj-1} < 0$	4.7%
$I_{it}=K_{itj-1} > 0:20$	38%
$I_{it}=K_{itj-1} > 0:25$	25%
$\text{corr}(I_{itj-1}; I_{it})$	0.008
$\text{corr}(I_{it}=K_{itj-1}; I_{itj-1}=K_{itj-2})$	0.30

## 3.2 Methodology

### 3.2.1 Estimation of the production function

The production function is given by

$$Y_{it} = A_{it} K_{it}^{\mu}$$

We estimate  $\mu$ , by regressing the log of real production on the log of the capital stock including time dummies and fixed effects. From our data  $\mu$  is estimated as 0.34, with a standard error of 0.08. One can show that our estimate of the slope of the production function,  $\mu$ ; is related to the markup (or price-cost marginal) of the firms (where markup or price cost margin is traditionally defined as price minus marginal cost over marginal cost). The markup is equal to  $\frac{\theta(1-\mu)}{\mu}$ , where  $\theta$  is the capital share in gross output.

Calculating the implied markup of our slope parameter estimate lets us gauge how reasonable it is. Assuming a capital share between 0.16 and 0.20, and combining it with our estimate of  $\mu$  (0.34), this leads to a markup between 31 and 39%. We are not aware of estimates of markups in German manufacturing. However, using four digit S.I.C. manufacturing industry level data for the U.S., Domowitz et al (1988) obtain an average markup of

37% which is similar to ours. They obtain these estimates of the markups using a methodology initially developed by Hall (1986). This methodology exploits the fact that the ratio of cost increase to output increase is equal to marginal cost. Hall (1986) uses the ratio of labor cost increases relative to output increases (correcting for technical progress) to estimate marginal cost and hence markups. Domowitz (1988) et al. show that Hall's estimates are too high due to the fact that he ignores material inputs. Domowitz (1988) et al. show that including material inputs reduces estimated margins by a factor  $(1-\theta_m)$ , with  $\theta_m$  the share of materials in gross output. More recently Morrison (1992) estimates markups for aggregate U.S. manufacturing in the range of 11% to 23 %. She deviates from former authors by using a production-theory framework where both labor and capital are quasi fixed. It is unresolved in the literature whether these estimates of markups using aggregate data can be compared with those from firm individual data. One of the reasons is that it is unclear whether the demand equation measured at the aggregate level is that of an industry or that of a representative firm. (For a discussion see Morrison (1992)).

### 3.2.2 Calculation and decomposition of the profit shocks

In principle one could use the profit and capital stock data to calculate the profit shocks  $A_{it}$ . However, we have noticed that measured profits are highly variable and therefore contain much measurement error.<sup>16</sup> One can show that in our theoretical model profits are equal to a fixed factor times the wage bill:

$$\pi(A_{it}; K_{it}) = c^\mu w_{it} L_{it} \quad (11)$$

So that we calculate the profit shocks (up to a multiplicative factor) using equation (1) and (11) as

$$A_{it} = c^\mu w_{it} L_{it} = K_{it}^\mu \quad (12)$$

We then decompose the profit shocks into a fixed component, and time varying component by regression the log of the profit shock on (a constant and) fixed effects.<sup>17</sup> :

<sup>16</sup>Note that this measurement error should not lead to a bias in the determination of  $\mu$  since it is measurement error in the "y-variable".

<sup>17</sup>Note that one can not identify the fixed effect from the constant  $c$  separately. However since we are not

$$\log(A_{it=c}) = \log(c) + a_i + \epsilon_{it} \quad (13)$$

The time varying components  $\epsilon_{it}$  are used in the investment regression. One can further split the time varying component of the shock into the aggregate and the idiosyncratic components:  $\epsilon_{it} = a_t + a_{it}$ . An analysis of variance decomposition of  $\epsilon_{it}$  into those two components reveals that practically all variation is due to the idiosyncratic time varying component.

Table 3. Features of the (firm demeaned) profit shocks (in logs): $\epsilon_{it}$
minimum: -0.80
maximum: 0.49
std. dev. $\epsilon_{it}$ : 0.118
std. dev. $a_t$ : 0.018
standard deviation $a_{it}$ : 0.118
autocorrelation $\epsilon_{it}$ : 0.48

### 3.3 The relationship between investment, profitability shocks and the leverage ratio.

We study the following relationship between investment, profitability and the leverage ratio.

$$i_{it} = \tilde{A}_0 + \tilde{A}_1 \epsilon_{it} + \tilde{A}_2 (\epsilon_{it})^2 + \tilde{A}_3 \text{ag}_{t-1} + \tilde{A}_4 B_{it} \text{gK}_{it} + \tilde{A}_5 (\epsilon_{it} B_{it} \text{gK}_{it})^2 + \eta_{it}$$

where  $i_{it}$  is the deviation of the investment rate at firm in year t from the firm specific mean,  $\epsilon_{it}$  is the demeaned profit shock,  $B_{it} \text{gK}_{it}$  is the demeaned leverage ratio and  $(\epsilon_{it} B_{it} \text{gK}_{it})$  is the product of both squared. This relationship was suggested by careful examination of the policy function for investment. Profitability shocks as well as variations

interested in the level of the parameter  $A_{it}$ , but rather its variation, this is irrelevant for our purposes. A oneway analysis of variance on the level of the profit shock (in logs)  $A_{it=c}$  across firms reveals that the estimated standard deviation of the firm specific profit shock is 0.98 (i.e the across firm variation of the firm specific effect), while the idiosyncratic (including time effect) has a standard deviation of 0.129. In the sample 98.8 % of the variation in the profit level (in logs) is across firms.

in the debt leverage ratio seem to have non-linear effects on investment. In particular, the last term was suggested by the observation that variations in the debt leverage ratio have effect on investment mostly when debt is high, capital is low and profitability is high. In simulations of the model we confirmed that small variations in the structural parameters produced large variations in the coefficients of the above reduced form regression. This is a necessary condition for identification of the structural parameters in the indirect inference procedure that we follow later in this paper.

Table 4. Summary Statistics of the regression variables

	mean	st.dev	min	max
$i_{it}$	0.00	0.13	-0.58	0.63
$\pi_{it}$	0.00	0.11	-0.80	0.46
$(\pi_{it})^2$	0.01	0.03	0.00	0.64
$\pi_{it-1}$	0.00	0.11	-0.52	0.49
$B_{it}g_{K_{it}}$	0.00	0.20	-1.24	0.87
$(\pi_{it}B_{it}g_{K_{it}})^2$	0.00	0.004	0.00	0.08

Table 5. Correlation matrix of the regression variables

	$i_{it}$	$\pi_{it}$	$(\pi_{it})^2$	$\pi_{it-1}$	$B_{it}g_{K_{it}}$	$(\pi_{it}B_{it}g_{K_{it}})^2$
$i_{it}$	1					
$\pi_{it}$	0.32	1				
$(\pi_{it})^2$	-0.04	-0.23	1			
$\pi_{it-1}$	-0.01	0.48	0.06	1		
$B_{it}g_{K_{it}}$	-0.27	-0.18	0.00	0.01	1	
$(\pi_{it}B_{it}g_{K_{it}})^2$	-0.08	0.09	0.38	0.09	-0.19	1

Table 4 gives the summary statistics of the regression variables. Table 5 gives the correlation matrix. The investment rate is positively correlated with the contemporaneous profit shock (correlation is 0.32) as one should expect and is negatively correlated with beginning of period leverage ratio (correlation is -0.27). Also the shocks are positively autocorrelated (correlation of the shock with its lag of 0.48). The profit shocks are also negatively correlated with the leverage ratio indicating that higher leveraged firms are more likely to face negative profit shocks. The lagged profit shock however is practically uncorrelated with the leverage ratio.

Table 6 gives the regression results. These show that there is an economically important relationship between the profit shocks the leverage ratio and investment. A 1 standard

deviation positive profitability shock (which implies an 11% increase in profits) increases the investment rate by 6.7 percentage points. The relationship is somewhat nonlinear: 5.9 percentage points is coming from the shock and 0.8 percentage points from the shock squared. (The calculation is  $0.11 \cdot 0.533 + 0.11 \cdot 0.11 \cdot 0.659$ ).

The negative coefficient on the product between the profitability shock and the leverage implies that the effect of a positive profitability shock on investment is dampened for firms with higher leverage. For instance a firm with a 1 standard deviation higher leverage (i.e. 0.20) the dampening effect would be 0.3 percentage points ( i.e.  $((0.11 \cdot 0.20)^2) \cdot 6.52$ ). Also, independently of the profitability shocks, firms with higher leverage invest less. A firm with a 1 standard deviation higher leverage (i.e. 0.20) has an investment rate that is lower by 0.3 percentage points.

Given the fact that in the data profitability shocks are highly correlated while the demeaned investment rate is not, it is not surprising that the lagged shock has a negative sign. Since a positive shock is likely to be followed by a positive shock this implies a dampened behavior of the investment rate.

TABLE 6: Regression of investment on profitability shocks and leverage

Coefficient	
$\alpha_{it}$	0.533* (0.056)
$(\alpha_{it})^2$	0.659* (0.157)
$\alpha_{it-1}$	-0.276* (0.054)
$B_{it} \cdot K_{it}$	-0.156* (0.025)
$(\alpha_{it} B_{it} \cdot K_{it})^2$	-6.52* (1.693)

\* significant at the 1% level. Robust standard errors (adj Rsq=0.22)

### 3.4 Using the distribution of the profitability shocks in simulating the model

The theoretical investment model can be simulated when its parameters ( $\mu; \sigma; \rho_s; \rho$ ) are given a value and the profitability shocks  $A_{it}$  are given a distribution. For the simulation, the distribution has to be discretised. One can abstract from the idiosyncratic fixed part of the profitability shock (without loss of generality we set it equal to 1 in the simulation)

	-0.48885	-0.14633	-0.07996	-0.04659	-0.0209	0.001595	0.022444	0.046227	0.079789	0.149245	0.328455	Total
-0.48885	<b>0.31</b>	0.31	0.12	0.10	0.00	0.00	0.00	0.05	0.07	0.00	0.05	100
-0.14633	0.10	<b>0.29</b>	0.28	0.13	0.03	0.05	0.02	0.01	0.07	0.02	0.00	100
-0.07996	0.04	0.19	<b>0.14</b>	0.17	0.14	0.05	0.08	0.07	0.06	0.03	0.01	100
-0.04659	0.03	0.07	0.10	<b>0.17</b>	0.14	0.18	0.08	0.14	0.06	0.03	0.01	100
-0.0209	0.02	0.08	0.11	0.17	<b>0.15</b>	0.15	0.12	0.08	0.10	0.03	0.01	100
0.001595	0.00	0.03	0.07	0.15	0.18	<b>0.18</b>	0.15	0.12	0.08	0.03	0.01	100
0.022444	0.02	0.03	0.05	0.09	0.18	0.09	<b>0.18</b>	0.17	0.14	0.04	0.01	100
0.046227	0.00	0.04	0.07	0.05	0.11	0.09	0.19	<b>0.17</b>	0.17	0.10	0.02	100
0.079789	0.03	0.04	0.04	0.02	0.06	0.08	0.13	0.13	<b>0.13</b>	0.26	0.07	100
0.149245	0.03	0.05	0.05	0.04	0.04	0.05	0.07	0.13	0.14	<b>0.26</b>	0.13	100
0.328455	0.05	0.00	0.02	0.00	0.05	0.02	0.00	0.02	0.15	0.37	<b>0.32</b>	100

Figure 1: Transition matrix

We discretise the distribution of the aggregate part of the productivity shock  $a_t$  and the time varying idiosyncratic part  $a_{it}$ : Since the standard deviation of the aggregate part is very small (0.02) compared with the standard deviation of the time-varying idiosyncratic part (0.12), we let the aggregate part only take on two values -0.02 and +0.02 (which imply  $A_t = 1:02$  or  $0:98$ ). The probability that a high aggregate shock is followed by a low one was calculated as 0.40. The transition matrix is given below.

Transition matrix aggregate part of productivity shock

	-0.02	0.02
-0.02	0.6	0.4
0.02	0.4	0.6

For the time varying idiosyncratic part  $a_{it}$  we discretised nonparametrically the empirical distribution into 11 bins (9 bins each containing 10 percent of the observations and two outlier bins each containing 5 percent of the observations). The transition matrix was also calculated nonparametrically.

The high probabilities at the diagonal and both above and below the diagonal reflect the high autocorrelation of the productivity shocks.

### 3.5 Structural Estimation

We proceed by fixing a priori some of the structural parameters of the model. In particular, we set  $r = 0:0413$ ;  $\bar{r} = 1/(1 + d)$ ;  $d = 0:0549$ ;  $\pm = 0:085$ ;  $p_b = 1$ ; and  $\mu = 0:34$ : The interest rate  $r$  has two functions in our model. First it is the remuneration interest rate for the firm if it has negative debt, i.e. if it accumulates funds. Second it is the lowest marginal interest rate at which the firm can borrow if it has zero debt. It is set at 4.13% which is the average

real yield on industry bonds in Germany over the period 1966-2002. The marginal interest rate for firms with positive debt is  $r + \frac{r}{p_S K_{it}} B_{it} + r \frac{B_{it}}{p_S K_{it}}$ . The discount rate is set at 5.49%. It is the average real yield on German stocks (measured by the DAX index) over the period 1966-2002. Taking the discount rate  $d$  higher than  $r$ , makes sure that a firm has an incentive to make dividend payments and not accumulate an infinite amount of assets. Say a firm makes positive profits, has no debt and has enough funds for investment. If  $r > d$  the firm simply accumulates funds and never pays them out. Note that if such a firm would never face negative shocks it would have an infinite value since the rate at which assets would accumulate  $r$  would be larger than the discount rate. Note that since we have  $d > r$ , the firm has an incentive to take positive debt to finance itself. Only taking positive debt can equate the discount rate with the marginal cost of debt finance.

The depreciation rate is based on our estimates with data from German manufacturing industry and is described in the Appendix. The profitability curvature parameter,  $\mu$ , was estimated from our data. The vector of remaining structural parameters to be estimated is called  $\xi = (\theta; \sigma; p_S; F)$ . We will estimate these using the indirect inference method.<sup>18</sup> This approach involves several well-defined steps.

First, we solve the firm's dynamic programming problem for arbitrary values of the structural parameters  $\xi$  and generate the corresponding optimal policy functions.<sup>19</sup> Second, we use these policy functions and arbitrary initial conditions to generate simulated data. In particular, we generate 14 artificial panels comprising data for 170 firms for 7 years. Third, this simulated data set is used to calculate the model analogues of the coefficients and/or moments we obtained using actual data. Letting  $a_{it} = \ln(A_{it})$ ; the reduced form regression on which we base our indirect inference is

$$\epsilon_{it} = \tilde{A}_1 e_{it} + \tilde{A}_2 (e_{it})^2 + \tilde{A}_3 \ln K + \tilde{A}_4 (e_{it} \ln K)^2 + u_{it} \quad (14)$$

<sup>18</sup>This approach was introduced by Gourieroux, and Monfort (1996), Gourieroux, Monfort and Renault (1993), and Smith (1993). The following are some examples of empirical papers using this approach. Cooper and Haltiwanger (2002) estimate an investment model with both convex and non-convex adjustment costs. Adda and Cooper (2002) study the impact of scrapping subsidies on new car purchases. The distribution of price adjustment costs are estimated by Willis (1999). Cooper and Ejarque (2001) investigate the role of market power in the Q theory.

<sup>19</sup>The problem is solved using the value function iteration method. Rust (1987a and 1987b) applied this method in his studies. Christiano (1990a and 1990b) showed that it method performs better than linear-quadratic approximation in the context of the stochastic growth model.

where  $r_{it}$  is the investment rate at firm  $i$  in period  $t$ , and  $B_{it}/K_{it}$  is the ratio of debt to the capital stock.<sup>20</sup> All variables are converted to deviations from their firm-specific means.

Cash flow for the simulated data is calculated according to

$$CF_{it} = \begin{cases} \frac{1}{2} [(A_{it}; K_{it})] (1+r)(1+r_{it})B_{it} + B_{it} & \text{when } B_{it} \geq 0 \\ [(A_{it}; K_{it})] rB_{it} & \text{when } B_{it} < 0 \end{cases} \quad (15)$$

Fourth, we check whether the distance between  $a^d$ ; the vector of coefficients from the actual data, and  $a^s(\epsilon)$ ; the vector of coefficients from data simulated given  $\epsilon$ ; are arbitrarily close. If they are not, update  $\epsilon$  in a manner that is likely to make this distance smaller and go back to the first step.

More formally, we try to minimize with respect to  $\epsilon$  the following quadratic function:

$$\min_{\epsilon} J(\epsilon) = (a^d - a^s(\epsilon))^T W (a^d - a^s(\epsilon))$$

where  $W$  is a weighting matrix.<sup>21</sup> In practice, we use the method of simulated annealing in order to minimize  $J(\epsilon)$ :<sup>22</sup>

### 3.6 Results

The point estimates of the structural parameters are given in Table 7 and look quite reasonable. The parameter  $\theta$  determines the external finance premium. An increase of the leverage ratio of 1 standard deviation, i.e. by 20 percentage points increases the external

<sup>20</sup>It is important that the moments and the coefficients used be responsive to changes in the underlying structural parameters of the model. When that is the case, as specified by Gourieroux and Monfort (1996), minimizing the distance between the simulated data moments and the actual data moments will generate consistent estimates of the structural parameters since the simulated moments depend on the structural parameters.

<sup>21</sup>Since the number of structural parameters is equal to the number of coefficients that we are trying to match we have many choices of matrix to use. An example is a  $4 \times 4$  diagonal matrix with ones. In the implementation we use the inverse of the variance-covariance matrix of  $a^d$ :

<sup>22</sup>There are a couple of advantages of this method compared to the conventional algorithms. First of all, this method explores the function's entire surface, and tries to optimize the function while moving both uphill and downhill. Thus it is almost independent of starting values. The other advantage of this method is that it can escape from local optima, and still find the global optimum by moving uphill and downhill. Further, the assumptions of the simulated annealing method regarding functional forms are less strict. Gøe, Ferrier, and Rogers (1994) provide evidence that this algorithm is quite good in finding the global optimum for difficult functions.

...nance premium by 0.56 percentage points (i.e. 56 basis points). The parameters  $\rho$  and  $F$  affect the cost of investing. The total cost of investment as a fraction of the capital stock is defined as:

$$C^b(K_{it}; I_{it}) = K_{it} = p \frac{I_{it}}{K_{it}} + \frac{\rho}{2} \frac{I_{it}^2}{K_{it}^2} + F$$
 At the mean investment rate of 0.19 the convex adjustment cost,  $\frac{\rho}{2} \frac{I_{it}^2}{K_{it}^2}$ , is 0.007, the fixed cost  $F$  is 0.021. In other words, when the investment rate is 0.19, total convex adjustment costs are 3.7 percent (or  $0.007/0.19$ ) of the purchase cost, total fixed cost are 10 percent of the purchase cost of investing ( $0.021/0.19$ ). Thus, it seems that fixed costs of adjustment are quantitatively more important than convex ones. There is also evidence of partial irreversibility as the resale price of installed capital is estimated to be around 83 percent the purchase price. However the resale price parameter is highly imprecise.

Table 7: Estimates of the structural parameters

Parameter	estimate	std.error
$\rho$	0.028	0.009
$\sigma$	0.405	0.025
$F$	0.021	0.004
$p_s$	0.830	21.09

Table 8: Regression of investment on profitability shocks and leverage: Actual versus simulated data

Coefficient	Data	Std. error	Model	Std.error	Difference
$\beta_{it}$	0.533	(0.056)	0.466	(0.008)	0.067
$(\beta_{it})^2$	0.659	(0.157)	0.531	(0.073)	0.128
$\alpha_1$	-0.276	(0.054)	-0.367	(0.007)	-0.091
$\beta_{it} \alpha_1$	-0.156	(0.025)	-0.148	(0.056)	0.008
$(\beta_{it} \alpha_1)^2$	-6.52	(1.693)	-4.789	(1.57)	1.731

Table 8 shows the regression coefficients of our reduced form regression of investment on the profitability shocks and leverage using the actual data and the simulated data (where the simulated data were obtained using the structural parameters as in Table 7). The table also reports the difference between the coefficients when using actual and simulated data. The coefficients of our reduced form investment regression using the actual data are reasonably well matched with those of regression using the simulated data. The coefficients of true and simulated data on the shock and the leverage ratio are less than 1 standard error (measured

by the actual data st. error) apart. The coefficients of the shock squared are practically 1 standard error apart. The worst ...t is found in the lagged shock and the interaction between the shock and the leverage ratio.

Table 9: Moments of actual data versus simulated data

	Data	Model
$\text{corr}(f_{it}; \epsilon_{it})$	0.33	0.25
$I_{it} = K_{it} - K_{it-1} > 0:20$	0.38	0.28
$\text{corr}(f_{it}; B_{it} / K_{it})$	-0.18	0.01
$\text{corr}(\epsilon_{it}; B_{it} / K_{it})$	-0.27	-0.01
$\text{corr}(g_{it-1}; \epsilon_{it})$	0.008	-0.34
$\text{corr}(B_{it} = K_{it} - g_{it-1}; K_{it-1})$	0.42	-0.20

Table 9 shows some other moments of the actual and simulated data. The contemporaneous correlation of the profitability shock with the investment rate is very similar between actual and simulated data implying that the model captures well this contemporaneous correlation. Also the nonlinear effect of the profitability shocks is well captured as evidenced by a similar fraction of firms having investment bursts. The contemporaneous correlation between the profitability shock and the leverage ratio is however not so well captured. Where it is negative in the actual data it is absent in the simulated data. Related to this, the contemporaneous correlation between the leverage ratio and the investment rate is much more negative in the data.

The dynamics of the simulated data seems to be different than the dynamics of the actual data. The autocorrelation of the investment rate is dramatically different. Where there is no autocorrelation in the actual data, there is a negative one in the simulated data. Also the autocorrelation of the debt ratio is highly positive in the actual data while it is negative in the simulated data. Trying to understand why this is the case, it is interesting to note that the interaction term between the leverage ratio and the shock is not well-matched by the model. It is possible that measurement error in the leverage ratio is the cause of some of the difference in dynamics. There is only one type of debt in the theoretical model. This debt also necessarily moves together with any investment or dividend decision that are partly explained by profitability shocks. In the data however firms have trade debt, trade credit, debt to finance inventories etc. These types of debt can move completely independently of

investment or dividend decisions. This could lead to such drastically different autocorrelation patterns in the actual versus simulated data.

## 4 APPENDIX: Sample Selection

The major source of the data is the AMADEUS database from Bureau Van Dijk (releases CD-rom June 2001 and September 1997). This is a database including firm balance sheet and profit and loss information for more than 30 European countries. We only use the information on the German firms. Our analysis is concentrated on the largest German manufacturing firms over the period 1992-1999.<sup>23</sup>

The elimination of the firms is conducted in a number of steps.

1. We only use consolidated accounts. This means that data are all on the group level (capital stock, assets, turnover, etc.) There are 1334 firms (manufacturing and non-manufacturing) which have at least 1 year of consolidated accounts. The reason why we concentrate on consolidated accounts are threefold. First, unconsolidated accounts can give a very misleading picture of the true nature of the firm. It is customary that the output of a large firm is usually produced over multiple plants, each (or a few taken together) with own legal identity and own unconsolidated account. For instance, BASF AG, has a consolidated turnover of around 30 billion euro, where it has an unconsolidated one of around 11 billion euro. Second, the true financial boundaries of the firms are the group not the individual plants. For instance for investment purposes, cash flow generated by one plant can easily be transferred to other plants. Third, limiting ourselves to consolidated data makes our study more comparable with US studies based on Compustat. Compustat contains consolidated data.

2. We only keep manufacturing firms which have at least 7 years of consecutive information on book value of capital stock and depreciation. This leads to 200 firms.

3. We only keep firms if they have profits and cash flow information. This leads to 170 firms

4. We do not use all observations. We checked on the websites of many companies and found that if the investment rate was higher than 0.9 (90%) this practically always was

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<sup>23</sup>Most German firms have only minor legal obligations to provide accounting information. This information is not sufficient to perform the study in this paper, since it does not include capital stock information. For instance, the June 2001 CD-rom contains accounting information on 39965 firms (both manufacturing and non-manufacturing firms), however 32832 have only limited accounting information. In general these firms are relatively small or are subsidiaries of larger firms.

measuring a merger or acquisition. We deleted all observations for which the investment rate was over 90% . We also deleted either the years before or after these investment rates of 90% (depending on what rendered the most data left over), to account for the fact that the firm could change substantially as a result of the merger or acquisition. This leads to our final dataset of 170 firms on 1163 observations. The dataset is unbalanced. However, each firm has at least 3 observations. On average, a firm has 6.8 observations. The maximum number of observations for a firm is 8.

These 170, firms are truly the larger ones. They had a total replacement value of capital stock of 101 billion euro in 1995 , where the total manufacturing industry in Germany had in 1995 a capital stock total of 483 billion euro.

## 4.1 Description of the variables:

### 4.1.1 Raw variables from the CD-rom:

FIAS: Fixed assets; represents the book value of all fixed assets of the firm, including building and structures, machinery and equipment, intangible fixed assets and financial fixed assets (share ownership in other companies)

OFAS: other fixed assets, are mainly financial fixed assets.

OPPL: operating profit or loss

DEPR: depreciation

PL: profit or loss of the year, is operating profits after exceptional items, taxation and interest payments.

STAF: wage bill of the firm

### 4.1.2 Constructed variables:

book value capital stock,  $K_t^b$  : The book value of the capital stock was constructed by the calculation FIAS-OFAS.

investment price deflator,  $P_t^I$ : was constructed by dividing aggregate industry investment data in current and prices of 1995.

investment at current prices,  $I_t^c$ : The AMADEUS database does not give gross investment figures directly. They have to be calculated using depreciation and capital stock numbers. We use the accounting identity:  $I_t^c = K_t^b - K_{t-1}^b + Dep_t$

real investment,  $I_t$ : is constructed as investment at current prices deflated by the investment price deflator  $I_t^c = P_t^I$ .

real capital stock  $K_t$ : The capital stock was constructed using the perpetual inventory method. The book value of the first year was multiplied by a factor  $1.26/P_t^I$  to convert the book value into replacement value at 1995 prices. The factor 1.26 was derived from aggregate German data by dividing the net capital stock in manufacturing at replacement prices by the net capital stock at historical acquisition prices. The depreciation rates were constructed using aggregate industry level data. The depreciation rates are between 6 and 13 percent. The average depreciation rate is 8.5 percent. The perpetual inventory formula used is  $K_t = (1 - \delta)K_{t-1} + I_t$

investment rate  $\frac{I_t}{K_{t-1}}$ : constructed as  $I_t$  divided by  $K_{t-1}$ :

real profits  $\pi_t$ : are constructed as operating profits plus depreciation (OPPL+DEPR) deflated by the German GDP-deflator.

real cash flow  $CF_{it}$ : are constructed as profits or loss plus depreciation (PL+DEPR) deflated by the German GDP-deflator.

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