

**Real-time Model Uncertainty in the  
United States:  
the FED from 1996-2003**

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**Discussion**

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## **Interesting paper!**

- Analyse important aspect of monetary policy in real time
- Not only data are revised, but also model

This has implication for assessment of the economy and for the formulation of optimal monetary policy

Model revisions may have larger impact than data revisions

- Nice !!!
- Huge task !!!
- Food for thought
- More of this will certainly come in the future (hopefully also from the ECB)

However ... I have one problem: the main result of the paper is a paradox!

*Model based optimal policy rules worked better before the major model changes introduced in 2001 to capture the productivity boom. After the changes it does worse than the historical rule*

How should we read this results?

Is model uncertainty such that model can become counterproductive? Should we get rid of models? What do policy makers know that modelers don't know?

This discussion tries to interpret this particular result of the paper

It has a reassuring conclusion ....

Consider 3 things in the paper:

## 1. The Rule (Taylor type)

$$r_t = \tilde{\pi}_t + rr_t^* + \alpha_\pi(\pi_t - \pi_t^*) + \alpha_y(y_t - y_t^*)$$

$rr_t^*$ : *equilibrium real interest rates/ “ad hoc”*  
endogenous, “slowly changing” variable

$$rr_t^* = (1 - 0.05)rr_t^* + 0.05(r_t - \pi_t)$$

## 2. Major model change in 2001

Introduce a stochastic (variable) trend to model potential output  $y^*$  / response to productivity booms of the nineties

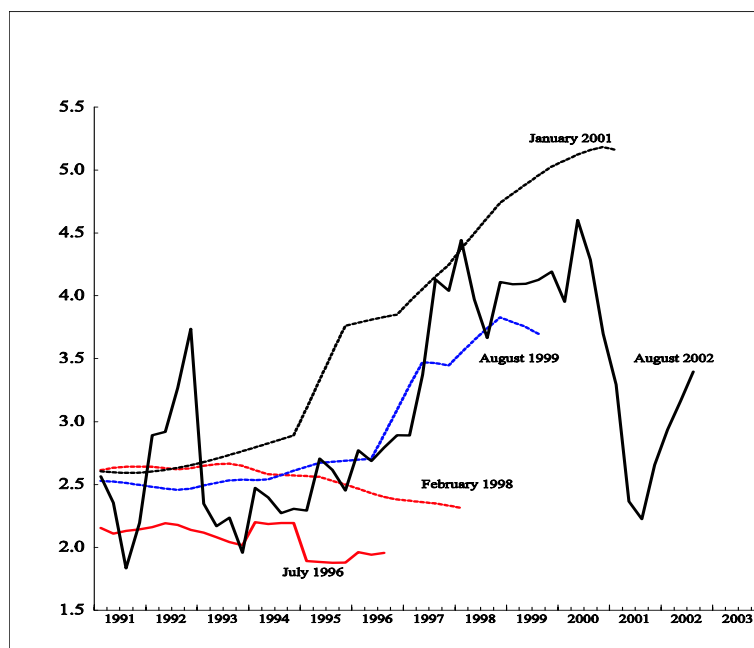
*productivity boom*  $\rightarrow \Delta y_t^*$  changes  
modellers realize it and introduce stochastic trend

**result**  $\rightarrow \Delta y_t^*$  become

- more correlated with cycle
- more volatile

Figure 1 and 2

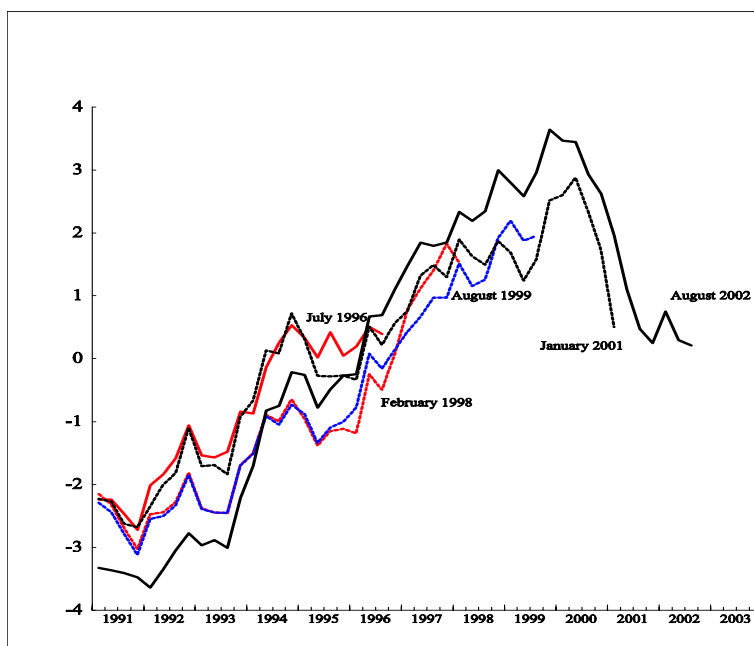
**Figure 1** Real-time 4-quarter non-farm potential output growth  
**Changes a lot in 2002**



**Figure 2**

Real-time GDP output gaps

**Do not change much!!!**



### 3. Result on policy rule

**Before 1997:** Taylor type (ad hoc and optimal) rules do better than historical rules

**2003 vintage:** Optimal rule becomes worse than historical rule

→ Tetlow: “Gap ( $y_t - y_t^*$ ) and inflation ( $\pi_t$ ) alone are not able to capture shocks to the growth rate of potential output ( $\Delta y_t^*$ ) which in turn affect equilibrium real interest rate ( $rr_t^*$ )”

$\Delta y_t^* \uparrow \Rightarrow rr_t^* \uparrow$  **not reflected** in  $y_t - y_t^*$  and  $\pi_t$

$\Rightarrow$  Optimal Taylor type rules do not work, however historical policy does!!



## **Question:**

what is the historical rule? Discretionary/non model based or alternative rule not considered in the paper?

## **Put 1-2-3 together**

Explore the conjecture that the historical rule is not Taylor type, but a rule (also simple) tracking the natural interest rate

## A. Observe:

The equilibrium rate  $rr_t^*$  component of the rule should be a function of the rate of growth of potential output  $\Delta y_t^*$  and should change with the changes introduced in 2001 (stochastic trend)

This is not done in the paper where  $rr_t^*$  is just a smooth function

Should allow  $rr_t^*$  to change with  $\Delta y_t^*$

$$rr_t^* = f(\Delta y_t^*)$$

## B. Explore an alternative rule to Taylor

### Telow/Taylor's rule

$$r_t = \tilde{\pi}_t + rr_t^* + \alpha_\pi(\pi_t - \pi_t^*) + \alpha_y(y_t - y_t^*)$$

Consider two alternative fits:

#### 1. Taylor fit

$$rr_t^* \approx \text{constant}$$

#### 2. Growth Rate Rule fit

$$rr_t^* \text{ moves with } \Delta y_t^*$$

→  $r_t$  moves with BOTH output gap and  $\Delta y_t^*$

To implement rule 2, (I don't have the model based  $\Delta y_t^*$ ) I approximate  $\Delta y_t^* + (y_t - y_t^*)$  by a  $k = 8$  quarters moving average:

$$\frac{1}{k} \sum_{j=1}^k \Delta y_{t-j} = \text{MA}_k(\Delta y_t)$$

**Remark:** Similar to Orphanides (1999) but motivation different: here we want to capture potential growth while Orphanides wants to get rid of measurement errors in Gap estimates

## Emprirics / the two alternative rules

- Data:

$\tilde{\pi}_t$	GDP deflator, annual inflation
$y_t - y_t^*$	Deviation of Real GDP from HP trend
$\Delta y_t$	Annualized Real GDP quarterly growth rate
$r_t$	Federal Funds Rate

- Parameters

Taylor rule:  $\alpha_y = \alpha_\pi = .5$ ,  $rr_t^* = 2$

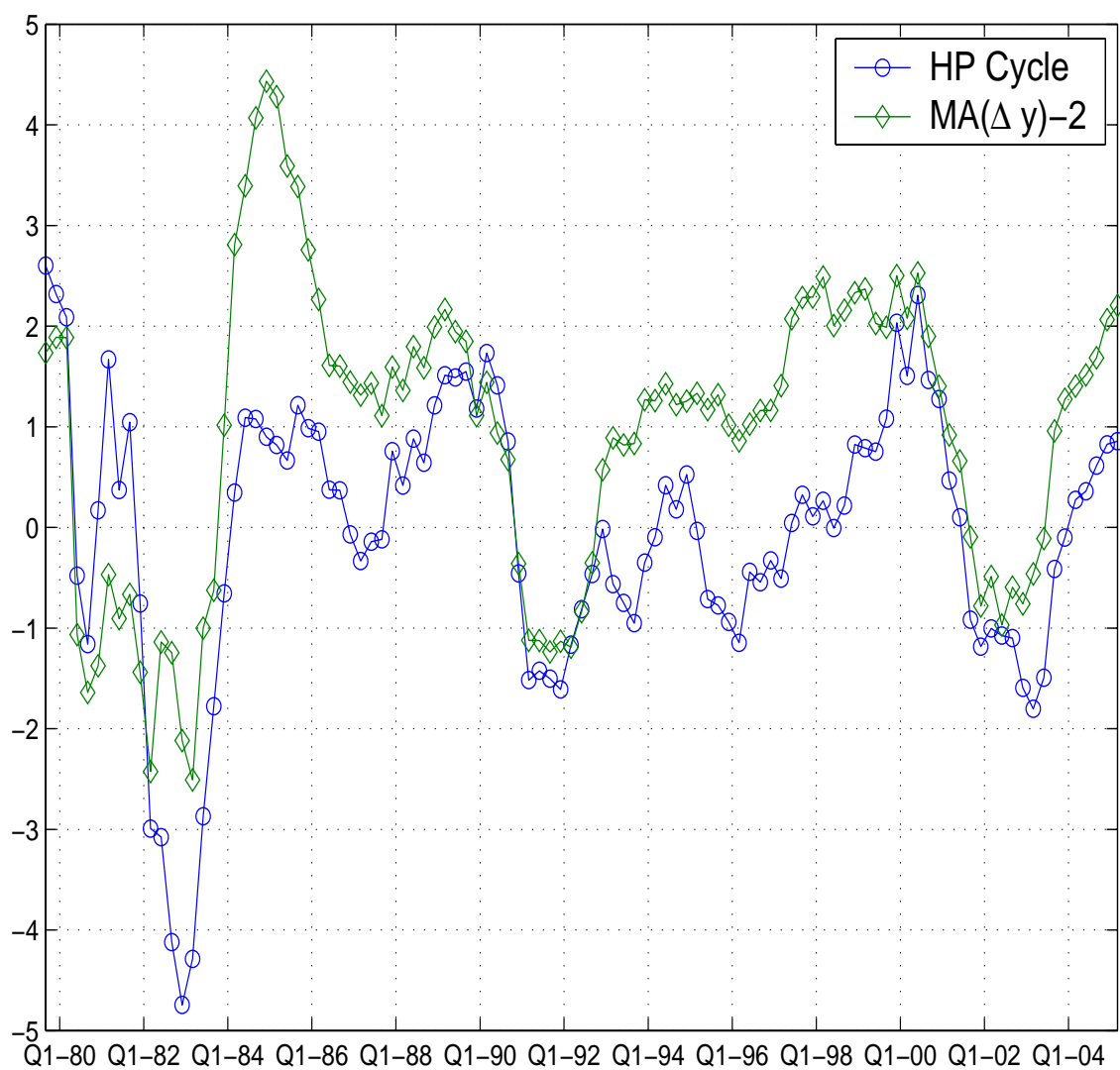
Growth rate rule:  $\alpha_\pi = .5$ ,  $k = 8$  quarters

- Sample

Volcker-Greenspan era: 1979Q3 - 2005Q1

# Figure 3

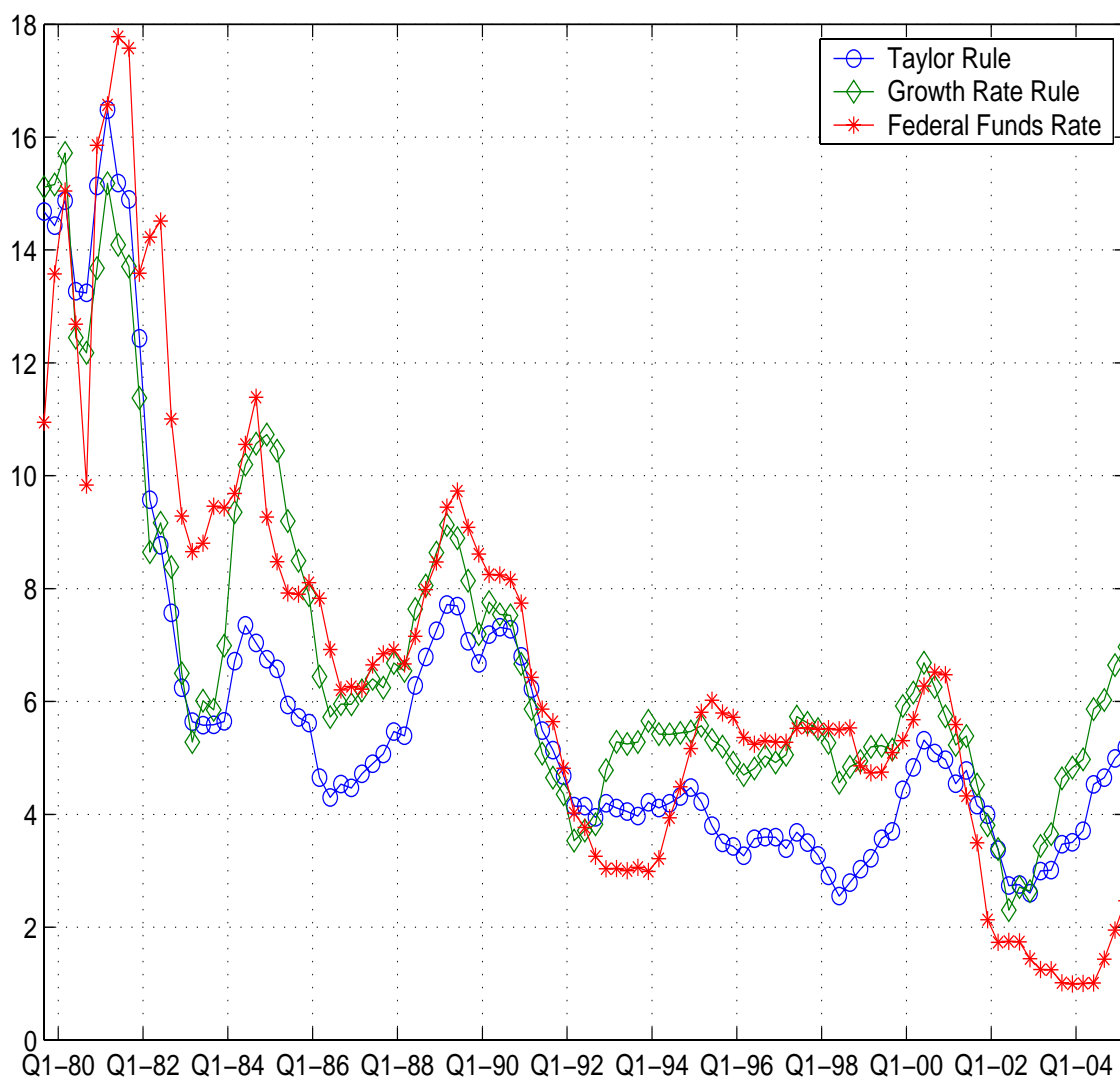
## Gap and Growth



**Very similar except in the period of productivity boom**

# Figure 4

## Rules



**During the period of productivity growth, the growth rate rule does better than Taylor**

## First conclusion

- The response of historical policy to the productivity boom can be captured by a simple rule – not considered in the exercise
- Simulations based on the FRB/US model do not capture it since the equation for the Equilibrium Real Rate of Interest is not compatible with the supply side of the model.
- Solution of the paradox? Model might be useful afterall

Lots of evidence points in that direction, however the rule should be tested on the FRB/US model (you should try)



## Another piece of the puzzle and more evidence for my story

One result of the paper is that, after the model changes in 2001, the optimal response to output implied by the Taylor rule jumps up (it asks for more responsiveness of policy to real/cyclical developments)  $\alpha_y^* \uparrow$

My explanation:

(i) The paper mispecifies  $rr_t^*$  by omitting its responsiveness to the higher volatility of the growth in potential output

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(ii) The model changes induce an increase in the correlation between the output gap and the growth of potential output



(i)+(ii) lead to an increase in  $\alpha_y^*$  (due to misspecification in  $rr_t^*$ )

$\Rightarrow$  this observation further supports our conjecture that results are due to miss-specification of the policy reaction function.

## More Evidence

Monetary Policy in Real Time, Giannone, Reichlin and Sala, NBER MACroeconomic Annual, 2005:

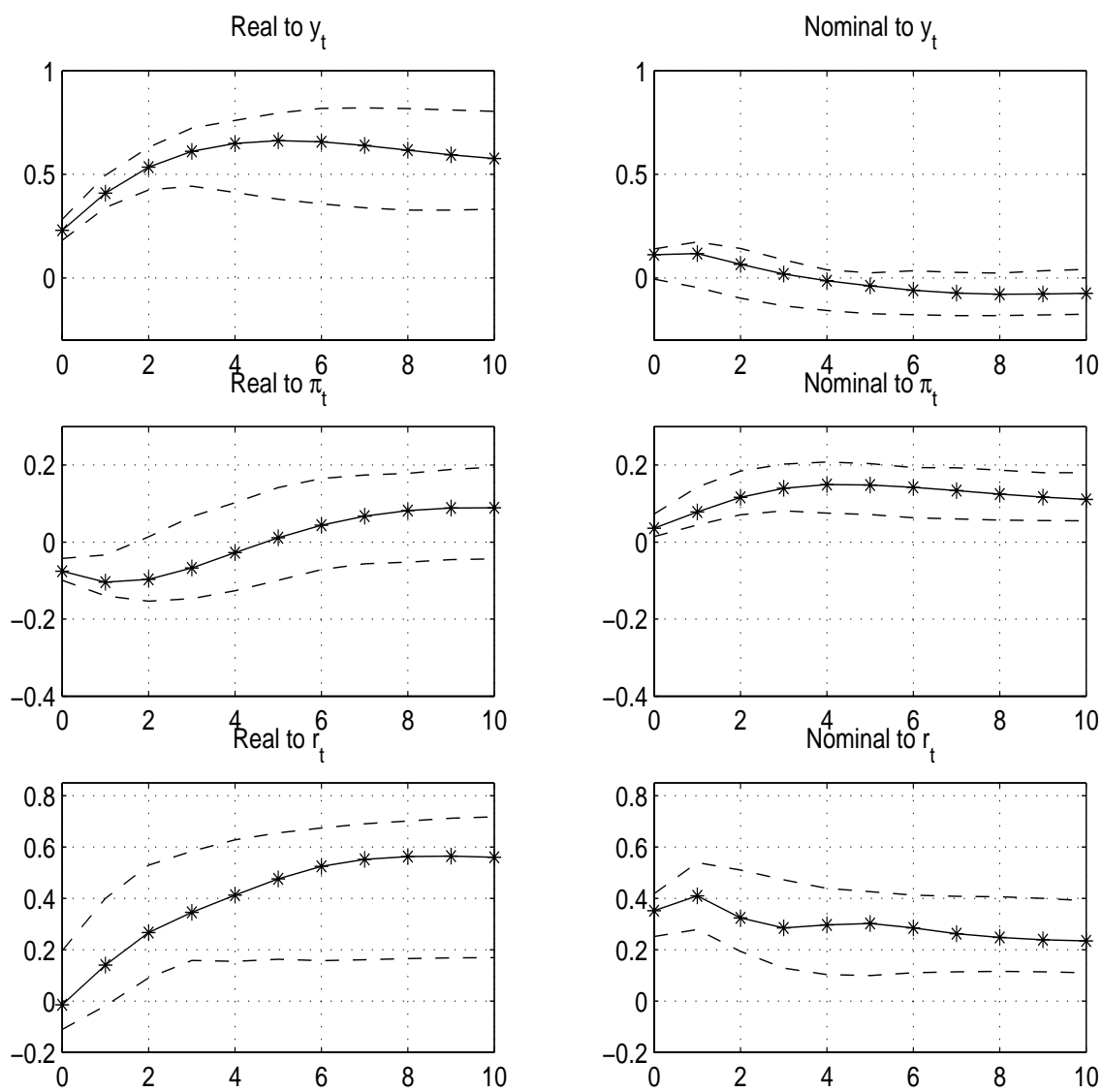
- Pseudo-real time estimates based on a large data set.
- Estimate response to two exogenous shocks: permanent/technology and transitory in output

### Results:

- nominal interest rate goes up persistently with the technology shock
- the real rate is correlated positively with and has the same shape of the permanent component of output

# Figure 5

## Impulse Response Functions from GRS, 2005



## Implications

- Reacting to real/persistent shocks the FED is able to adjust to changes of the Natural Rate of interest.
- In “normal” periods this policy cannot be identified from traditional rules since permanent changes of output cannot be identified from changes of the output gap.
- Policy reactions to changes of the growth rate of potential output do not add any additional (discretionary) dimension to the policy problem which can be still characterized by simple systematic behaviour.

## **Conclusions?**

We might still learn from models after all ...