

Interest Rates and Investment Redux

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May 2006

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Investment and the Cost of Capital

► Monetary policy:

- Policymakers use leverage over short-term market interest rates to influence the cost of capital.
- Changes in the cost of capital affect interest-sensitive components of aggregate demand.

► Fiscal policy:

- Elasticity of investment demand w.r.t. user cost of capital is the key parameter in determining the costs and benefits of alternative corporate tax policies.

► Little consensus regarding elasticity of investment demand:

- Published estimates range from 0 to -2.
- “Accelerator” variables (e.g., output, cash flow) have a much larger impact on capital spending than the user cost of capital.

Empirical Challenges

◉ Key Components of the User Cost:

- Required real rate of return (including a risk premium)
- Depreciation rate
- Price of new capital goods (including expected price changes)
- Tax terms (tax rate, PDV of depreciation allowances, ITC)

◉ Aggregate Time-Series Evidence:

- Simultaneity between interest rates and investment demand
- Price of capital and depreciation have little cyclical variation
- Many tax changes are transitory

◉ Firm-Level Evidence:

- Credit constraints
- Investment irreversibility constraints

Our Paper

- ▶ Estimate the relationship between firm-level investment decisions and *firm-specific* marginal external financing costs.
- ▶ Measure firm-specific external financing costs with prices of outstanding senior unsecured bonds traded in the secondary market.
- ▶ Cross-sectional heterogeneity in external financing costs?
 - Differences in default risk
 - Differences in recovery rates
 - Differences in external finance premiums due to capital market imperfections
 - Differences in liquidity premiums

Key Results

- ▶ Investment spending is highly sensitive to movements in *firm-specific* external financing costs:
 - 1 pp. increase in financing costs \Rightarrow decline in investment rate between 70–130 bps.
- ▶ Interest-sensitivity of investment demand is robust to:
 - Inclusion of various measures of expected future profits
 - Inclusion of *firm-specific* measures of expected default risk
 - Inclusion of cash flow and other liquidity variables
 - Alternative sample periods

Data Sources

- ◉ **Compustat:** firm-level income and balance sheet data
(1973–2004, fiscal year-end)
- ◉ **Lehman/Warga & Merrill Lynch:** prices of outstanding corporate bonds traded in the secondary market
(Jan1973–Dec2004, month-end)
- ◉ **Moody's/KMV:** expected default frequencies (EDFs)
(Jan1990–Dec2004, month-end)
- ◉ **BEA:** 2-digit SIC measures of depreciation and price of capital
(1987–2004, year-end)
- ◉ **Panel Dimensions:** 6,293 bonds issued by 1,131 firms over the 1973–2004 period

Bond Yields

- ▶ Month-end option-adjusted yields on outstanding long-term corporate bonds.
- ▶ U.S. nonfarm, nonfinancial issuers only.
- ▶ Senior unsecured issues only.
- ▶ Term-premium adjustment for each bond on each day
- ▶ Nominal yields converted to real yields using
 - Past realized inflation
 - Survey measures of expected inflation

Corporate Bond Characteristics

Table 1: Summary Statistics of Key Bond-Specific Variables

Variable	Mean	SD	Min	Med	Max
# of bonds per firm/month	3.28	4.01	1.00	2.00	57.00
Mkt. Value of Issue (\$mil.)	266.9	298.1	1.2	197.8	6,771.1
Maturity (years)	13.8	9.4	2.0	10.0	50.0
Effective Duration (years)	6.58	2.89	0.01	6.28	19.54
Composite Rating (S&P)	-	-	D	A3	AAA
Coupon Rate (%)	7.83	2.19	0.00	7.59	17.50
Nominal Yield (%)	8.52	2.89	0.17	8.05	35.31
Real Yield (%)	4.96	2.60	-4.07	4.74	29.99

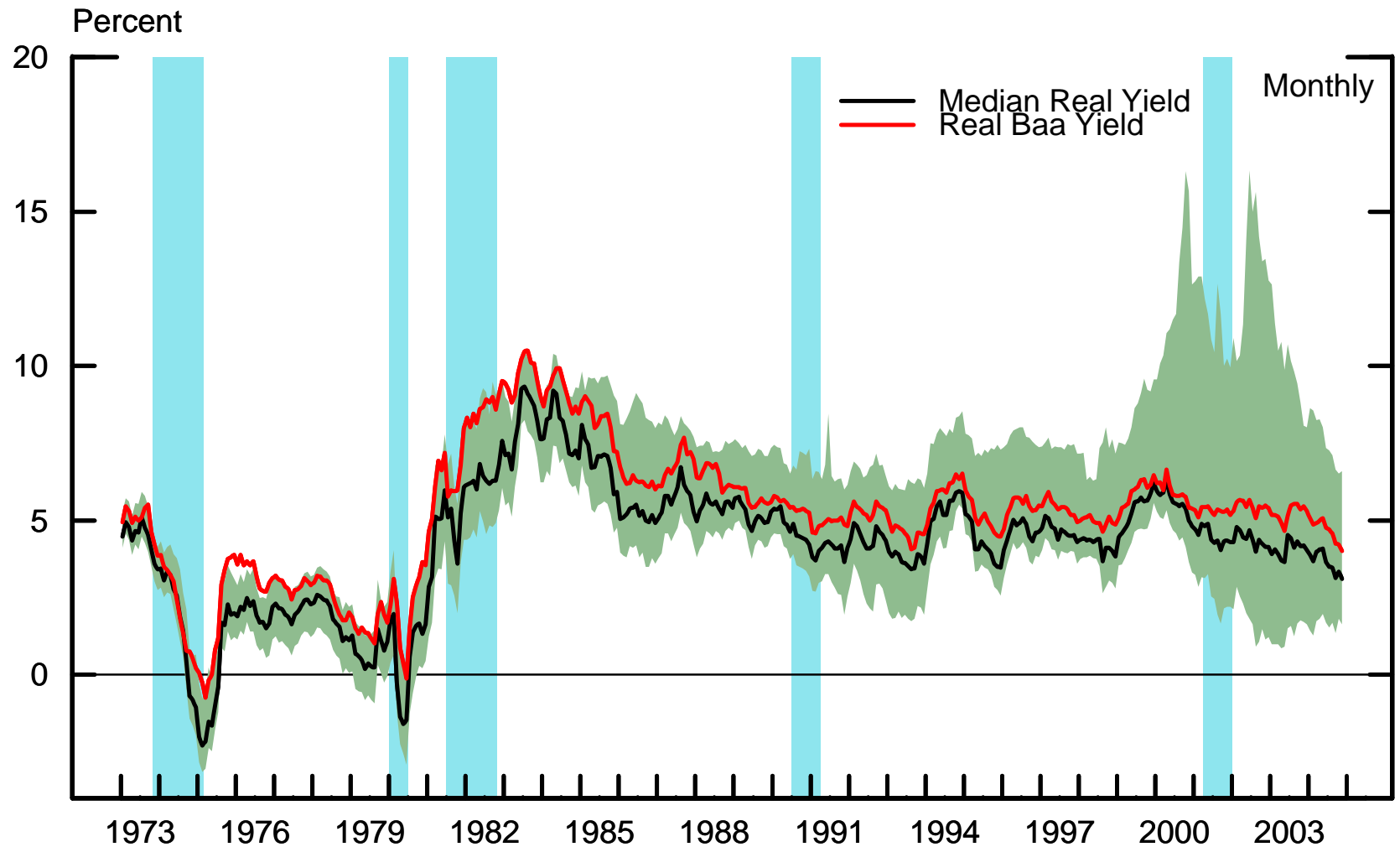
Panel Dimensions

Obs. = 374,747 $N = 6,293$ bonds

Min. Tenure = 1 Median Tenure = 45 Max. Tenure = 302

Corporate Bond Characteristics

Figure 1: The Evolution of Real Bond Yields



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Firm Characteristics

Table 2: Summary Statistics for Key Firm-Specific Variables

Variable	Mean	SD	Min	Med	Max
Sales (\$bil.)	8.36	16.78	< .00	3.41	245.0
Mkt. Capitalization (\$bil.)	8.27	18.98	< .00	2.62	297.7
Par Value to L-T Debt	0.44	0.25	< .00	0.41	1.00
Real Interest Rate (%)	5.51	3.08	-2.42	5.04	29.92
Investment to Capital	0.21	0.14	< .00	0.18	1.00
Sales to Capital	3.66	3.26	0.13	2.81	24.81
Profits to Capital	0.46	0.36	-0.20	0.37	2.50
Tobin's Q	1.49	0.78	0.45	1.26	15.25

Panel Dimensions

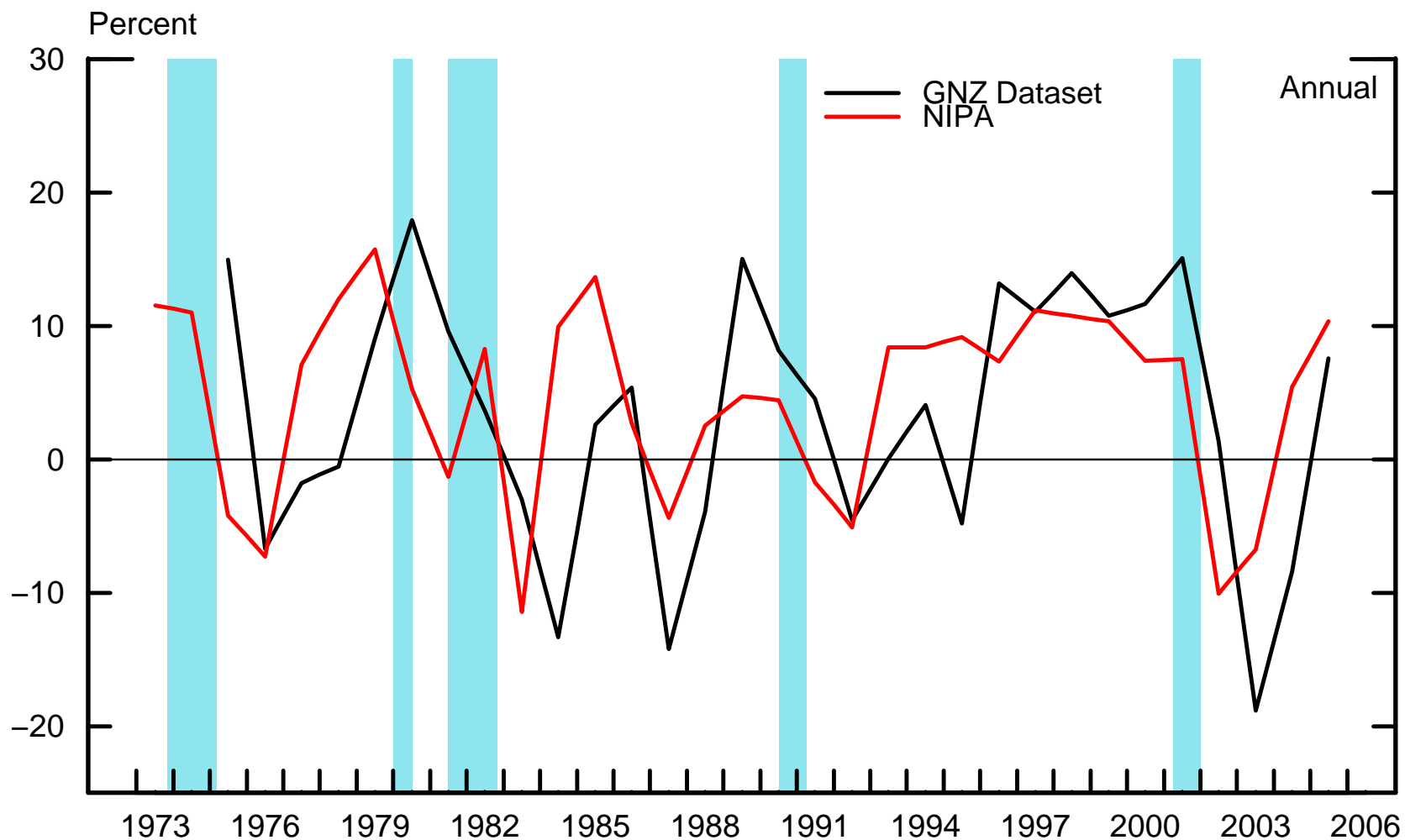
Obs. = 9,993 $N = 1,131$ firms

Min. Tenure = 1 Median Tenure = 6 Max. Tenure = 32

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Comparing Data with Broader Aggregates

Figure 2: The Growth of Real Business Fixed Investment



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Expected Default Risk

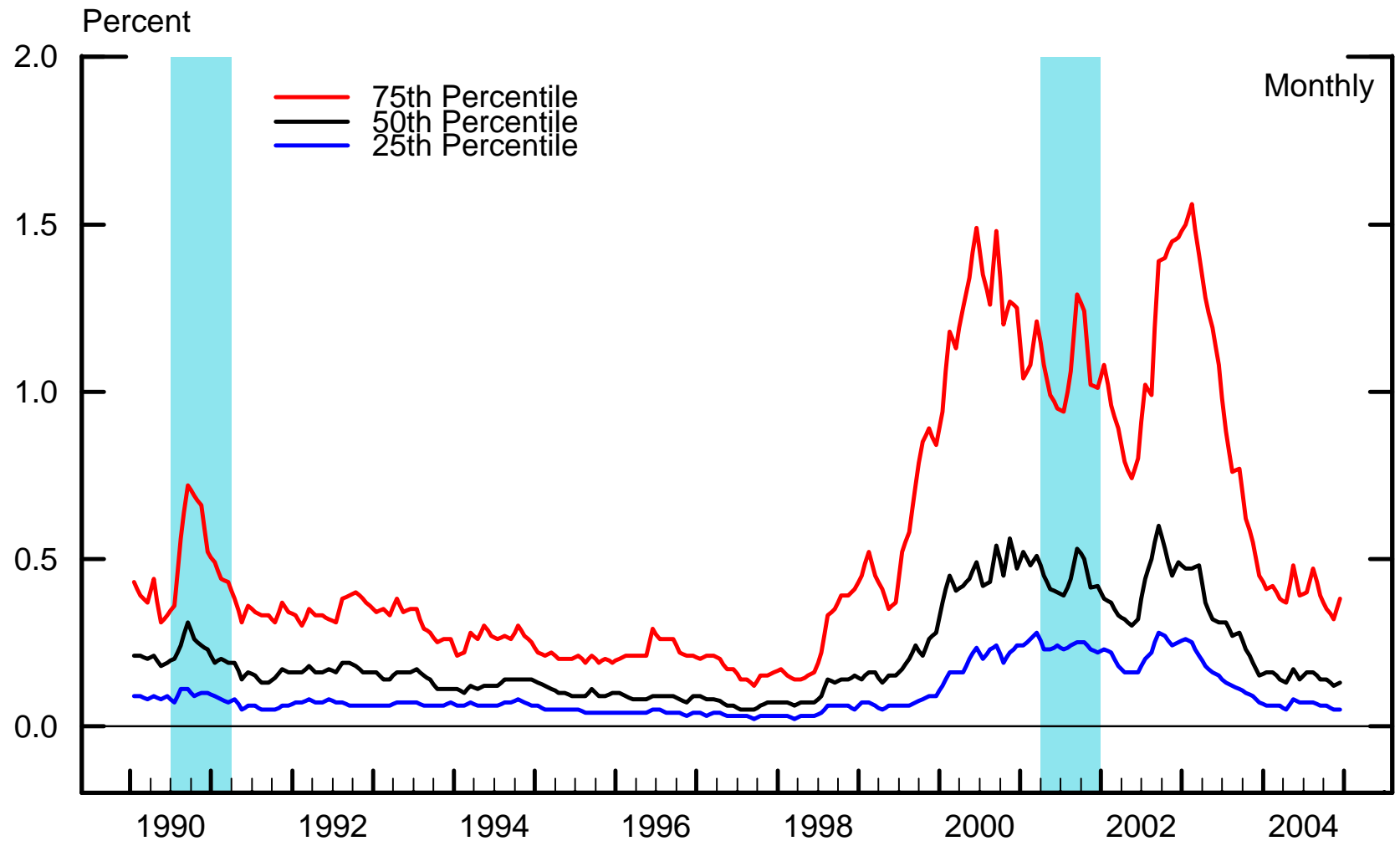
- ◆ **Default Probabilities:** expected default frequencies (EDFs)
 - Option-theoretic approach to calculate a firm-specific distance to default (DD):

$$\left[\begin{array}{c} \text{Distance} \\ \text{to Default} \end{array} \right] = \frac{\left[\begin{array}{c} \text{Mkt. Value} \\ \text{of Assets} \end{array} \right] - \left[\begin{array}{c} \text{Default} \\ \text{Point} \end{array} \right]}{\left[\begin{array}{c} \text{Mkt. Value} \\ \text{of Assets} \end{array} \right] \times \left[\begin{array}{c} \text{Asset} \\ \text{Volatility} \end{array} \right]}.$$

- Use actual defaults used to construct a statistical mapping from DD to EDF.
- The resulting EDF measures the likelihood that that a firm will default over the subsequent 12 months.

Expected Default Risk

Figure 3: The Evolution of Year-Ahead EDFs



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Neoclassical User Cost of Capital

- User cost of capital for firm j in industry s :

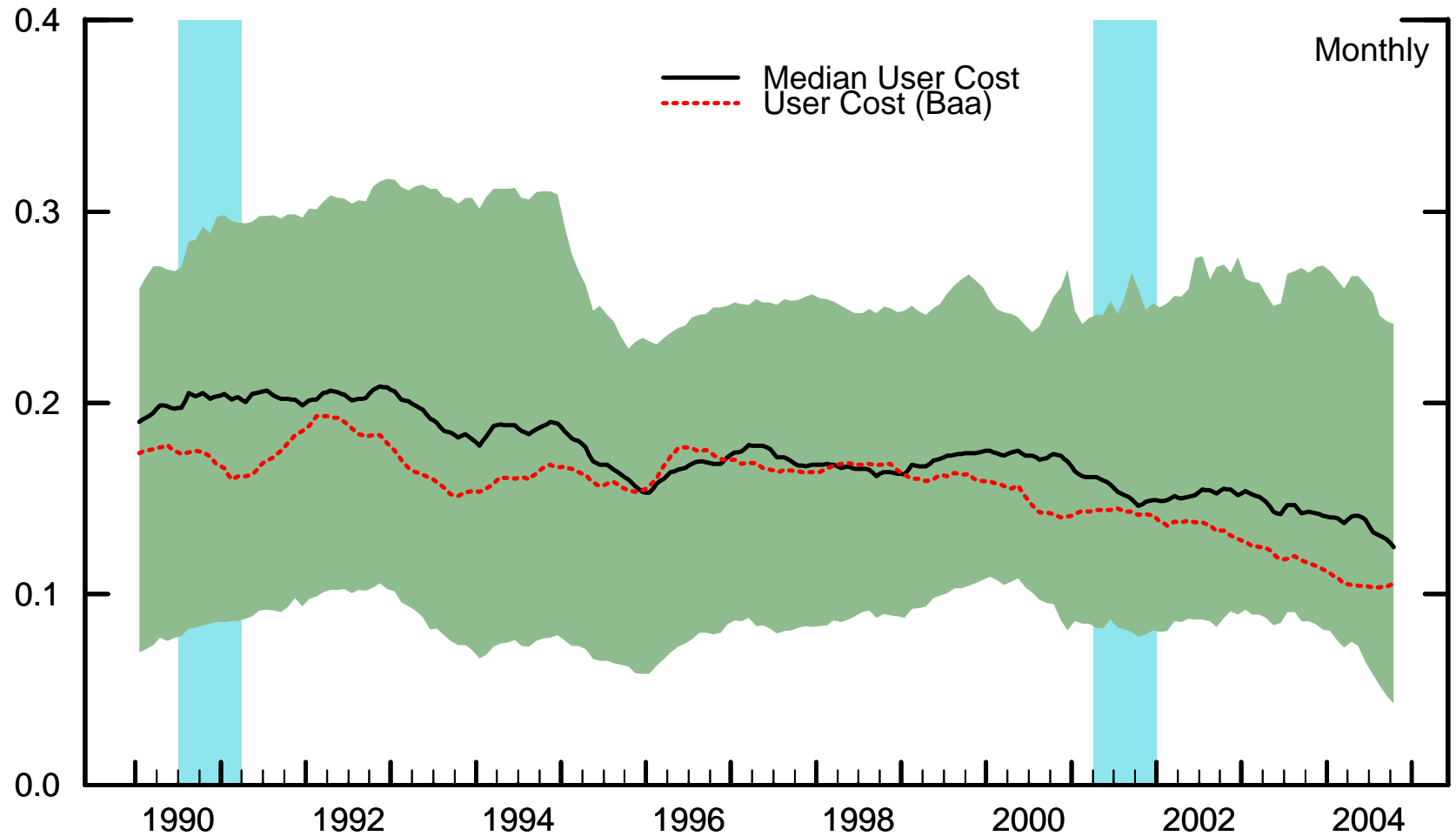
$$C_{jt}^K = \frac{P_{st}^K}{P_{st}^Q} \left[(1 - \tau_t) i_{jt} + \delta_{st} - E_t \left(\frac{\Delta P_{s,t+1}^K}{P_{st}^K} \right) \right] \left[\frac{1 - \tau_t z_{st}}{1 - \tau_t} \right]$$

- P_{st}^K / P_{st}^Q = relative price of capital goods
- $(1 - \tau_t) i_{jt}$ = after-tax *nominal* interest rate
- τ_t = corporate tax rate (common to all firms)
- δ_{st} = depreciation rate
- z_{st} = present discounted value of depreciation deduction

- Industry-level components $(P_{st}^K, P_{st}^Q, \delta_{st}, z_{st})$ aggregated from asset-level data (25 E&S and 5 NRS types).

User Cost of Capital

Figure 4: The Evolution of the User Cost



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Econometric Methodology

◆ Baseline Specification:

$$\frac{I_{jt}}{K_{j,t-1}} = \beta' Z_{jt} + \theta FC_{jt} + \eta_j + \lambda_t + \epsilon_{jt}$$

- $I_{jt}/K_{j,t-1}$ = investment rate in period t
- Z_{jt} = vector of investment fundamentals in period t
(sales-to-capital ratio, Tobin's Q, lagged investment rate)
- FC_{jt} = measure of external financing costs in period t
(real interest rate, neoclassical user cost)
- η_j = fixed firm effect
- λ_t = fixed time effect

◆ Sample Periods: 1974–2004; 1991–2004 (sub-sample)

◆ Estimation Methods:

- OLS Within/First-Difference
- First-Difference Dynamic GMM

OLS-Within Estimates

Table 3: Level Specification (1974–2004)

Dependent Variable: I_t/K_{t-1}				
S_t/K_{t-1}	0.028 (0.003)	0.021 (0.003)	-	-
Q_{t-1}	-	-	0.052 (0.007)	0.036 (0.006)
Π_{t-1}/K_{t-2}	-	0.111 (0.012)	-	0.131 (0.012)
r_t	-0.878 (0.131)	-0.699 (0.131)	-0.828 (0.126)	-0.636 (0.122)
$\Pr > W_\lambda$	< .001	< .001	< .001	< .001
BIC	-0.904	-0.941	-0.866	-0.917
Adj. R^2	0.509	0.527	0.489	0.516

First-Difference GMM

Table 4: Dynamic Specification (1974–2004)

Dependent Variable: $\Delta(I_t/K_{t-1})$				
$\Delta(I_{t-1}/K_{t-2})$	0.324 (0.028)	0.295 (0.029)	0.328 (0.027)	0.276 (0.028)
$\Delta(S_t/K_{t-1})$	0.037 (0.006)	0.034 (0.005)	-	-
ΔQ_{t-1}	-	-	0.040 (0.008)	0.040 (0.007)
$\Delta(\Pi_{t-1}/K_{t-2})$	-	0.031 (0.019)	-	0.065 (0.017)
Δr_t	-1.295 (0.365)	-1.212 (0.341)	-1.093 (0.335)	-1.185 (0.312)
$\Pr > m_1 $	< .001	< .001	< .001	< .001
$\Pr > m_2 $	0.518	0.574	0.521	0.523
$\Pr > J_N$	1.00	1.00	1.00	1.00

OLS-Within Estimates

Table 5: Level Specification (1991–2004)

Dependent Variable: I_t/K_{t-1}						
S_t/K_{t-1}	0.031 (0.003)	0.031 (0.003)	0.026 (0.003)	-	-	-
Q_{t-1}	-	-	-	0.047 (0.007)	0.046 (0.006)	0.036 (0.006)
EDF_{t-1}	-	-0.446 (0.120)	-0.395 (0.119)	-	-0.415 (0.122)	-0.368 (0.120)
Π_{t-1}/K_{t-2}	-	-	0.088 (0.014)	-	-	0.100 (0.014)
r_t	-0.680 (0.141)	-0.436 (0.158)	-0.340 (0.160)	-0.717 (0.140)	-0.492 (0.157)	-0.382 (0.157)
$\Pr > W_\lambda$	< .001	< .001	< .001	< .001	< .001	< .001
BIC	-0.975	-0.984	-1.014	-0.925	-0.932	-0.969
Adj. R^2	0.575	0.580	0.592	0.553	0.557	0.573

First-Difference GMM

Table 6: Dynamic Specification (1991–2004)

Dependent Variable: $\Delta(I_t/K_{t-1})$						
$\Delta(I_{t-1}/K_{t-2})$	0.410 (0.039)	0.398 (0.038)	0.381 (0.039)	0.394 (0.036)	0.383 (0.036)	0.372 (0.039)
$\Delta(S_t/K_{t-1})$	0.037 (0.009)	0.038 (0.008)	0.036 (0.007)	-	-	-
ΔQ_{t-1}	-	-	-	0.037 (0.007)	0.035 (0.007)	0.037 (0.007)
ΔEDF_{t-1}	-	-0.207 (0.185)	-0.208 (0.176)	-	-0.296 (0.171)	-0.299 (0.169)
$\Delta(\Pi_{t-1}/K_{t-2})$	-	-	0.002 (0.024)	-	-	-0.006 (0.020)
Δr_t	-1.306 (0.455)	-0.753 (0.396)	-0.817 (0.378)	-1.033 (0.402)	-0.724 (0.359)	-0.841 (0.353)
$\text{Pr} > m_1 $	< .001	< .001	< .001	< .001	< .001	< .001
$\text{Pr} > m_2 $	0.645	0.694	0.716	0.539	0.597	0.621
$\text{Pr} > J_N$	0.957	0.983	0.767	0.978	0.971	0.735

OLS-Within Estimates

Table 7: Level Specification (1991–2004)

Dependent Variable: I_t/K_{t-1}						
S_t/K_{t-1}	0.032 (0.003)	0.031 (0.003)	0.027 (0.003)	-	-	-
Q_{t-1}	-	-	-	0.049 (0.007)	0.046 (0.007)	0.036 (0.006)
EDF_{t-1}	-	-0.544 (0.112)	-0.466 (0.110)	-	-0.541 (0.112)	-0.460 (0.108)
Π_{t-1}/K_{t-2}	-	-	0.090 (0.014)	-	-	0.102 (0.013)
C_t^K	-0.270 (0.073)	-0.182 (0.069)	-0.153 (0.065)	-0.251 (0.079)	-0.165 (0.074)	-0.136 (0.067)
$\Pr > W_\lambda$	< .001	< .001	< .001	< .001	< .001	< .001
BIC	-0.963	-0.980	-1.012	-0.910	-0.927	-0.965
Adj. R^2	0.570	0.578	0.592	0.547	0.555	0.572

Measurement Error in C_t^K

Table 8: First-Difference 2SLS Estimates (1991–2004)

Dependent Variable: I_t/K_{t-1}						
$\Delta(S_t/K_{t-1})$	0.037 (0.003)	0.037 (0.003)	0.037 (0.003)	-	-	-
ΔQ_{t-1}	-	-	-	0.050 (0.006)	0.049 (0.005)	0.048 (0.006)
ΔEDF_{t-1}	-	-0.352 (0.104)	-0.332 (0.105)	-	-0.307 (0.102)	-0.304 (0.103)
$\Delta(\Pi_{t-1}/K_{t-2})$	-	-	0.035 (0.012)	-	-	0.005 (0.011)
ΔC_t^K	-0.782 (0.190)	-0.656 (0.152)	-0.623 (0.194)	-0.794 (0.174)	-0.689 (0.177)	-0.685 (0.177)
$\text{Pr} > W_{\Delta\lambda}$	< .001	< .001	< .001	< .001	< .001	< .001
BIC	-1.826	-1.837	-1.840	-1.752	-1.759	-1.756

Measurement Error in C_t^K

Table 9: First-Difference Dynamic GMM Specification (1991–2004)

Dependent Variable: $\Delta(I_t/K_{t-1})$						
$\Delta(I_{t-1}/K_{t-2})$	0.420 (0.040)	0.412 (0.038)	0.391 (0.040)	0.383 (0.034)	0.372 (0.034)	0.387 (0.040)
$\Delta(S_t/K_{t-1})$	0.031 (0.009)	0.033 (0.008)	0.031 (0.007)	-	-	-
ΔQ_{t-1}	-	-	-	0.035 (0.007)	0.034 (0.007)	0.038 (0.007)
ΔEDF_{t-1}	-	-0.271 (0.152)	-0.296 (0.143)	-	-0.180 (0.151)	-0.292 (0.140)
$\Delta(\Pi_{t-1}/K_{t-2})$	-	-	-0.006 (0.024)	-	-	0.031 (0.023)
ΔC_t^K	-1.100 (0.447)	-0.753 (0.342)	-0.759 (0.309)	-1.378 (0.369)	-1.199 (0.308)	-1.030 (0.269)
$\text{Pr} > m_1 $	< .001	< .001	< .001	< .001	< .001	< .001
$\text{Pr} > m_2 $	0.580	0.646	0.672	0.461	0.502	0.565
$\text{Pr} > J_N$	0.970	0.970	0.801	0.989	0.962	0.434

Directions for Future Research

- Investigate the source(s) of interest rate heterogeneity.
- Incorporate firm-specific interest rates into structural investment models.
- Joint modeling of debt and investment dynamics.